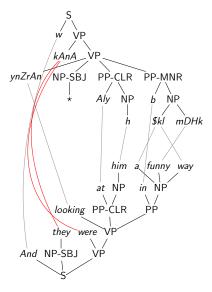
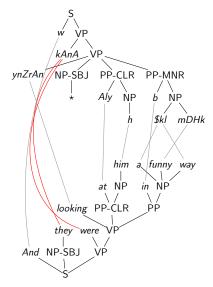
# The Power of Regularity-Preserving Multi Bottom-up Tree Transducers

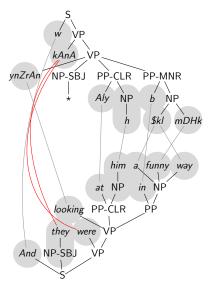
Andreas Maletti

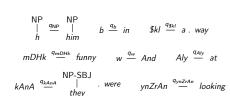
maletti@ims.uni-stuttgart.de

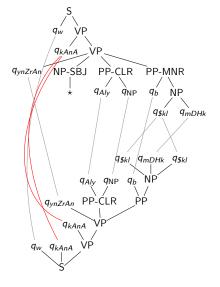
Gießen — August 2, 2014



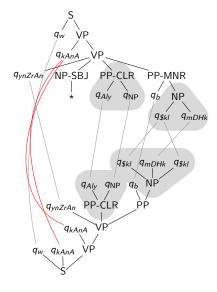


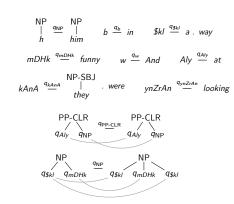


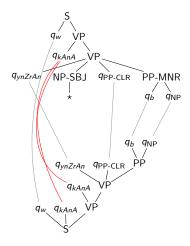


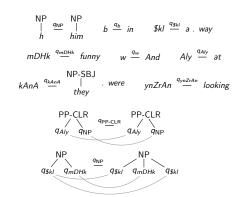


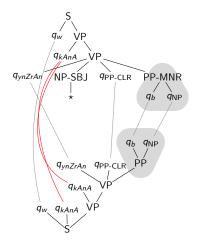


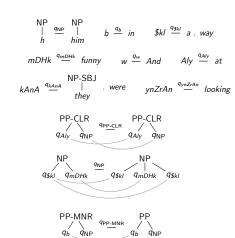




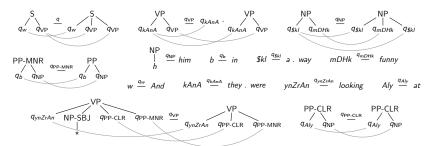








#### Extracted rules



#### Definition (MBOT)

linear extended multi bottom-up tree transducer  $(Q, \Sigma, I, R)$ 

- finite set Q states
- ullet alphabet  $\Sigma$  input and output symbols
- $I \subseteq Q$  initial states
- finite set  $R \subseteq T_{\Sigma}(Q) \times Q \times T_{\Sigma}(Q)^*$  rules
  - each  $q \in Q$  occurs at most once in  $\ell$   $(\ell, q, \vec{r}) \in R$
  - each  $q \in Q$  that occurs in  $\vec{r}$  also occurs in  $\ell$   $(\ell, q, \vec{r}) \in R$

#### Definition (Syntactic properties)

MBOT  $(Q, \Sigma, I, R)$  is

- linear extended top-down tree transducer with regular look-ahead (XTOP<sup>R</sup>) if  $|\vec{r}| \leq 1$   $\forall (\ell, q, \vec{r}) \in R$
- linear extended top-down tree transducer (XTOP) if  $|\vec{r}| = 1$  $\forall (\ell, q, \vec{r}) \in R$

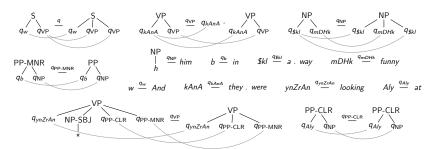
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- linear extended top-down tree transducer (XTOP) if  $|\vec{r}| = 1$   $\forall (\ell, q, \vec{r}) \in R$
- $\varepsilon$ -free if  $\ell \notin Q$

$$\forall (\ell, q, \vec{r}) \in R$$

#### Extracted rules



#### **Properties**

XTOPR:

XTOP: X



 $\varepsilon$ -free:  $\checkmark$ 



# Another Example

Example (textual)

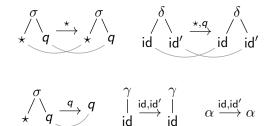
MBOT  $M = (Q, \Sigma, \{\star\}, R)$ 

- $Q = \{\star, q, \mathsf{id}, \mathsf{id}'\}$
- $\Sigma = \{\sigma, \delta, \gamma, \alpha\}$
- the following rules in R:

$$\begin{split} \sigma(\star,q) &\stackrel{\star}{\longrightarrow} \sigma(\star,q) & \quad \sigma(\star,q) \stackrel{q}{\longrightarrow} q \\ \delta(\mathsf{id},\mathsf{id}') &\stackrel{\star,q}{\longrightarrow} \delta(\mathsf{id},\mathsf{id}') & \quad \gamma(\mathsf{id}) \stackrel{\mathsf{id},\mathsf{id}'}{\longrightarrow} \gamma(\mathsf{id}) & \quad \alpha \stackrel{\mathsf{id},\mathsf{id}'}{\longrightarrow} \alpha \end{split}$$

# Another Example

#### Graphical representation



### **Properties**

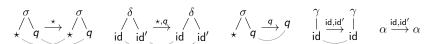
XTOP<sup>R</sup>: ✓

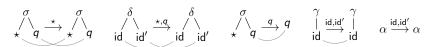




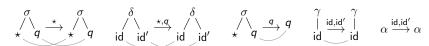




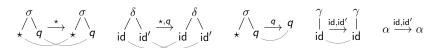


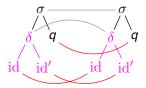


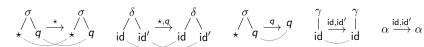


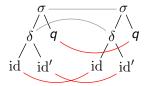




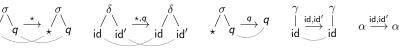








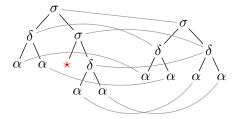




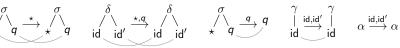


$$\begin{matrix} \gamma & \gamma & \gamma \\ | & \underline{\mathsf{id}}, \underline{\mathsf{id}}' & | \\ \mathrm{id} & & \underline{\mathsf{id}}\end{matrix}$$

$$\alpha \xrightarrow{\mathsf{id},\mathsf{id}'} \alpha$$



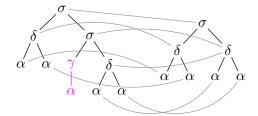


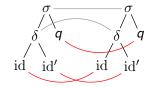




$$\begin{matrix} \gamma & \gamma & \gamma \\ | & id, id' & | \\ id & & id \end{matrix}$$

$$\alpha \stackrel{\mathsf{id},\mathsf{id}'}{\longrightarrow} \alpha$$





### Definition (sentential forms)

$$\langle t, A, D, u \rangle$$

- $t \in T_{\Sigma}(Q)$
- $A \subseteq \mathbb{N}^* \times \mathbb{N}^*$
- $D \subseteq \mathbb{N}^* \times \mathbb{N}^*$
- $u \in T_{\Sigma}(Q)$

input tree active links (red)

disabled links (gray)

output tree

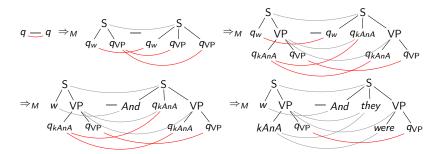
### Definition (Generation step)

$$\langle t, A, D, u \rangle \Rightarrow_{M} \langle t', A', D', u' \rangle$$

if and only if  $\exists q \in Q$ ,  $\exists v \in pos(t)$  labeled by q, and  $\exists \ell \stackrel{q}{\to} \vec{r} \in P$ 

- $|\vec{r}| = |A(v)|$  and  $\vec{w} = A(v)$
- $t' = t[\ell]_{\nu}$  and  $u' = u[\vec{r}]_{\vec{w}}$
- $A' = (A \setminus L) \cup \mathsf{links}_{v,\vec{w}}(\ell \stackrel{q}{\to} \vec{r}) \text{ and } D' = D \cup L \text{ with }$

$$L = \{(v, w) \mid w \in A(v)\}$$



#### Definition

state-computed dependencies:

$$M_q = \{ \langle t, D, u \rangle \mid t, u \in T_{\Sigma}, \langle q, \{(\varepsilon, \varepsilon)\}, \emptyset, q \rangle \Rightarrow_{M}^{*} \langle t, \emptyset, D, u \rangle \}$$

• computed dependencies:

$$\operatorname{dep}(M) = \bigcup_{q \in I} M_q$$

#### Definition

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computed dependencies:

$$dep(M) = \bigcup_{q \in I} M_q$$

computed transformation:

$$\tau_{M} = \{(t, u) \mid \langle t, D, u \rangle \in \operatorname{dep}(M)\}\$$

### Definition (Regularity-preserving)

```
transformation \tau \subseteq T_{\Sigma} \times T_{\Sigma} preserves regularity if \tau(L) = \{u \mid (t, u) \in \tau, t \in L\} is regular for all regular L \subseteq T_{\Sigma}
```

rp-MBOT = class of all regularity preserving transformations computable by MBOT

#### Compositions

- $\tau_1$ ;  $\tau_2 = \{(s, u) \mid \exists t : (s, t) \in \tau_1, (t, u) \in \tau_2\}$
- support modular development
- allow integration of external knowledge sources
- occur naturally in query rewriting

#### Known:

- $XTOP^R \subsetneq MBOT$
- MBOT is closed under composition
- all  $\tau \in \mathsf{XTOP}^\mathsf{R}$  preserve regularity

#### Known:

- XTOP<sup>R</sup> ⊆ MBOT
- MBOT is closed under composition
- all  $\tau \in \mathsf{XTOP}^\mathsf{R}$  preserve regularity

#### Question:

Is 
$$(XTOP^R)^* \subsetneq rp\text{-}MBOT$$
?  $(XTOP^R)^* \subseteq rp\text{-}MBOT$  is true 
$$(XTOP^R)^* = \bigcup_{k \geq 1} \underbrace{XTOP^R \; ; \; \cdots \; ; \; XTOP^R}_{k \; factors}$$

#### Motivation

- we use regularity-preserving MBOT for efficiency in our translation systems
- their power is currently not well understood

#### Motivation

- we use regularity-preserving MBOT for efficiency in our translation systems
- their power is currently not well understood
- e.g. general MBOT can handle discontinuities
- Is this still possible with regularity-preserving MBOT?
   or do they have the same power as compositions of XTOP

#### Contents

The problem

Linking technique

Results

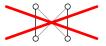
# Properties of Dependencies

### Definition (Hierarchical properties)

A dependency  $\langle t, D, u \rangle$  is

- input hierarchical if
  - 1.  $w_2 \not< w_1$
  - 2.  $\exists (v_1, w_1') \in D \text{ with } w_1' \leq w_2$

for all  $(v_1, w_1), (v_2, w_2) \in D$  with  $v_1 < v_2$ 





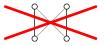
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- strictly input hierarchical if
  - 1.  $v_1 < v_2$  implies  $w_1 \le w_2$
  - 2.  $v_1 = v_2$  implies  $w_1 \le w_2$  or  $w_2 \le w_1$

for all  $(v_1, w_1), (v_2, w_2) \in D$ 

### Definition (Distance properties)

A dependency  $\langle t, D, u \rangle$  is

• input link-distance bounded by  $b \in \mathbb{N}$  if for all  $(v_1, w_1), (v_1v', w_2) \in D$  with |v'| > b  $\exists (v_1v, w_3) \in D$  such that v < v' and  $1 \le |v| \le b$ 



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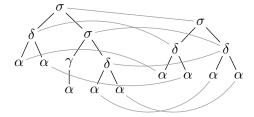
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- strict input link-distance bounded by b if for all  $v_1, v_1v' \in pos(t)$  with |v'| > b  $\exists (v_1v, w_3) \in D$  such that v < v' and  $1 \le |v| \le b$







strictly input hierarchical



strictly input hierarchical and strictly output hierarchical



strictly input hierarchical and strictly output hierarchical with strict input link-distance 2



strictly input hierarchical and strictly output hierarchical with strict input link-distance 2 and strict output link-distance 1

	hierarchical		link-distance bounded	
${\sf Model} \setminus {\sf Property}$	input	output	input	output
XTOP <sup>R</sup> MBOT	strictly ✓	strictly strictly	<b>√</b> ✓	strictly strictly

# Linking Theorem for $\varepsilon$ -free XTOP<sup>R</sup>

#### **Theorem**

Let  $M_1, \ldots, M_k$  be  $\varepsilon$ -free XTOP<sup>R</sup> over  $\Sigma$  such that

$$\{(c[t_1,\ldots,t_n],\,c'[t_1,\ldots,t_n])\mid t_1,\ldots,t_n\in\mathcal{T}\}\subseteq\tau_{M_1}\,;\cdots\,;\tau_{M_k}$$

for some contexts  $c, c' \in C_{\Sigma}(X_n)$  and special  $T \subseteq T_{\Sigma}$ .

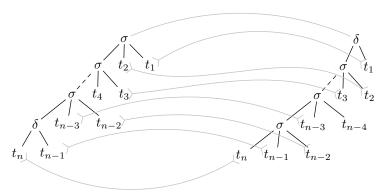
$$\forall 1 \leq i \leq k, \ \forall 1 \leq j \leq n$$
  
 $\exists t_j \in T, \ \exists \langle u_{i-1}, D_i, u_i \rangle \in \mathsf{dep}(M_i), \ \exists (v_{ji}, w_{ji}) \in D_i \ such \ that$ 

- $u_0 = c[t_1, \ldots, t_n]$  and  $u_k = c'[t_1, \ldots, t_n]$
- $pos_{x_j}(c') \leq w_{jk}$
- $v_{ji} \leq w_{j(i-1)}$  if  $i \geq 2$
- $pos_{x_j}(c) \leq v_{j1}$

## Linking Theorem for $\varepsilon$ -free XTOP<sup>R</sup>

### Corollary [see Sect. 3.4 in [Arnold, Dauchet 1982]]

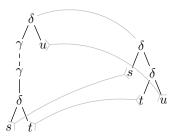
The illustrated tree transformation  $\tau$  cannot be computed by any  $\varepsilon\text{-free XTOP}^{\mathsf{R}}$ 



# Linking Theorem for $\varepsilon$ -free XTOP<sup>R</sup>

### Corollary [see Thm. 5.2 in [Maletti et al. 2009]]

The illustrated tree transformation  $\tau$  cannot be computed by any  $\varepsilon\text{-free XTOP}^{\mathsf{R}}$ 



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#### Example

• It rained yesterday night.

Topicalized: Yesterday night, it rained.

#### Example

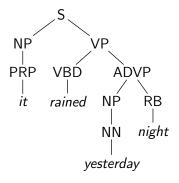
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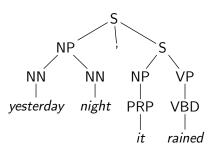
Topicalized: Yesterday night, it rained.

• We toiled all day yesterday at the restaurant that charges extra for clean plates.

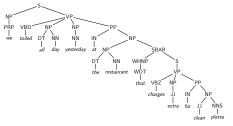
Topicalized: At the restaurant that charges extra for clean plates, we toiled all day yesterday.

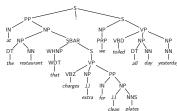
### Example (on the tree level)



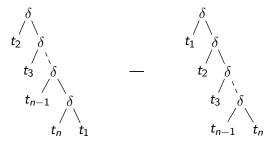


### Example (on the tree level)





## Abstract Topicalization



## Abstract Topicalization

#### Theorem

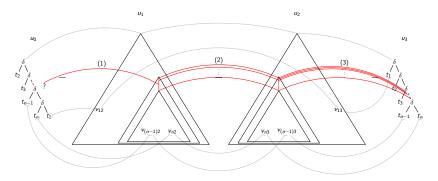
Abstract topicalization

- preserves regularity and
- can be computed by an MBOT

### Abstract Topicalization

#### Theorem

Abstract topicalization cannot be computed by any composition chain of  $\varepsilon$ -free XTOP<sup>R</sup>



### Consequence

Corollary

$$(\mathsf{XTOP}^\mathsf{R})^* \subsetneq \mathsf{rp}\text{-}\mathsf{MBOT}$$

## Linking Theorem for $\varepsilon$ -free MBOT

#### Theorem

Let  $M = (Q, \Sigma, I, R)$  be an  $\varepsilon$ -free MBOT such that

$$\{(c[t_1,\ldots,t_n],\,c'[t_1,\ldots,t_n])\mid t_1,\ldots,t_n\in\,T\}\subseteq\tau_M$$

for some contexts  $c, c' \in C_{\Sigma}(X_n)$  and special  $T \subseteq T_{\Sigma}$ .

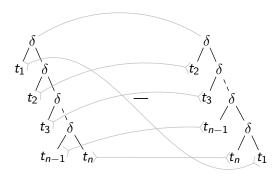
 $\forall 1 \leq j \leq n, \ \exists t_j \in T, \ \exists \langle u, D, u' \rangle \in \mathsf{dep}(M), \ \exists (v_j, w_j) \in D \ \textit{with}$ 

- $u = c[t_1, ..., t_n]$  and  $u' = c'[t_1, ..., t_n]$
- $pos_{x_j}(c) \leq v_j$
- $pos_{x_i}(c') \leq w_j$

### Linking Theorem for $\varepsilon$ -free MBOT

#### Corollary

Inverse of topicalization cannot be computed by any  $\varepsilon$ -free MBOT



# Summary & References

#### Summary

- 1.  $(XTOP^R)^* \subsetneq rp\text{-}MBOT$
- 2. rp-MBOT not closed under inverses
- 3. What happens to invertable MBOT?

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#### References

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