

Statistik für Digital Humanities

Gemischte ANOVA (GLM 5/5)

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Gemischte ANOVA

Bekannt:

- (einfaktorielle) ANOVA: Experiment durch Veränderung einer unabhängigen Variable (Gruppenzuordnung)
- ANCOVA: Experiment durch Veränderung einer unabhängigen Variable (Gruppenzuordnung) unter Eliminierung einer Variable außerhalb des Experiments
- Mehrfaktorielle ANOVA: Experiment durch Veränderung mehrerer unabhängigen Variablen (Gruppenzuordnungen)
- Abhängige ANOVA: Experiment durch Veränderung einer abhängigen Variable

Jetzt:

- Gemischte ANOVA: Experiment durch Veränderung (mindestens) einer abhängigen und einer unabhängigen Variable

Mehrfaktorielle ANOVA

Wir schauen uns jetzt eine dreifaktorielle gemischte ANOVA als Anschauungsbeispiel an.

Bibliotheken

```
install.packages("ez")  
install.packages("ggplot2")  
install.packages("nlme")  
install.packages("pastecs")  
install.packages("reshape")
```

```
#Initiate packages  
library(ez)  
library(ggplot2)  
library(nlme)  
library(pastecs)  
library(reshape)
```

Daten

| Gender | High Charisma | Low Charisma | Dullard |
|--------|-----------------|-----------------|-----------------|
| | Att — Avg — Ug | Att — Avg — Ug | Att — Avg — Ug |
| Male | 86 — 84 — 67 | 88 — 69 — 50 | 97 — 48 — 47 |
| | ... — ... — ... | ... — ... — ... | ... — ... — ... |
| Female | 89 — 91 — 93 | 88 — 65 — 54 | 56 — 48 — 52 |
| | ... — ... — ... | ... — ... — ... | ... — ... — ... |

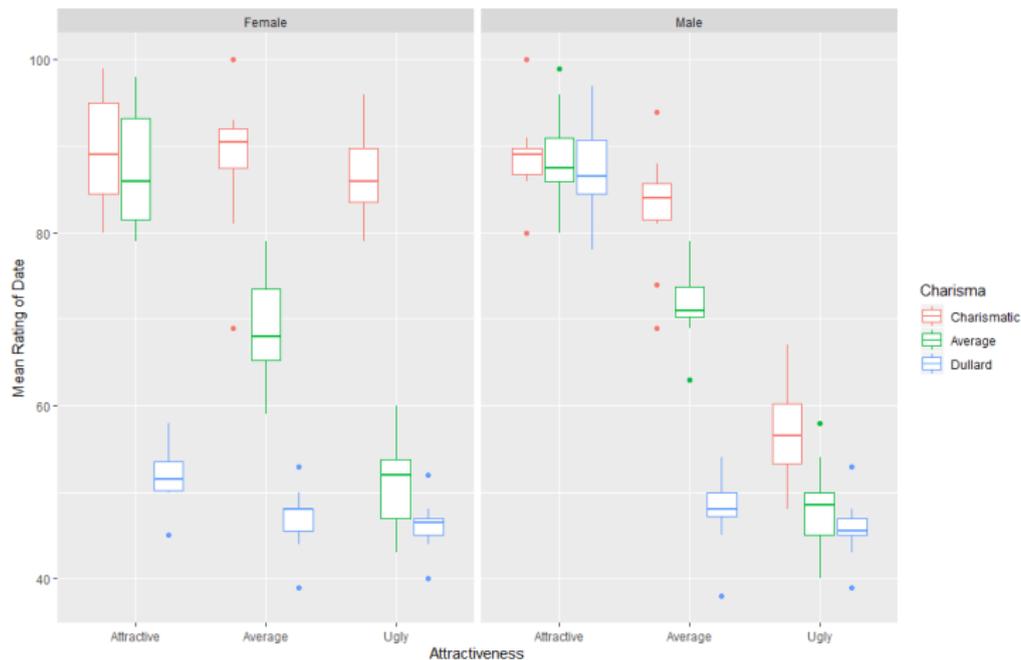
Moodle: LooksOrPersonality.dat

```
dateData<-read.delim("LooksOrPersonality.dat", header = TRUE)
speedData<-melt(dateData, id = c("participant","gender"), measured = c("att_high",
  "av_high", "ug_high", "att_some", "av_some", "ug_some", "att_none", "av_none",
  "ug_none"))
names(speedData)<-c("participant", "gender", "groups", "dateRating")
speedData$personality<-gl(3, 60, labels = c("Charismatic", "Average", "Dullard"))
speedData$looks<-gl(3,20, 180, labels = c("Attractive", "Average", "Ugly"))
speedData<-speedData[order(speedData$participant),]
```

Daten

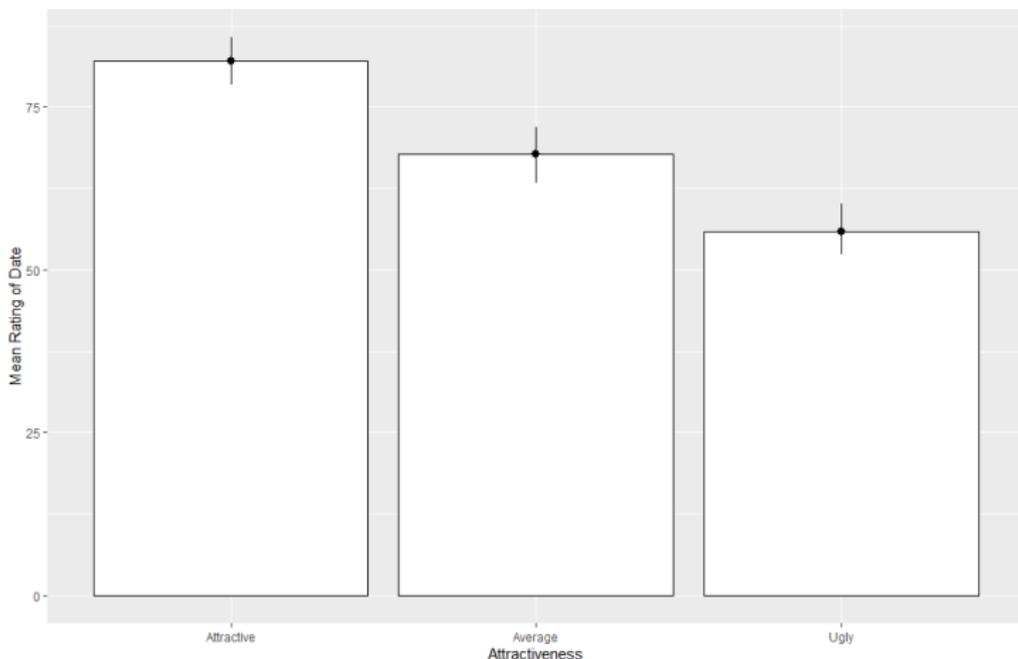
| participant | gender | groups | dateRating | personality | looks |
|--------------------|---------------|---------------|-------------------|--------------------|--------------|
| P01 | Male | att_high | 86 | Charismatic | Attractive |
| P01 | Male | av_high | 84 | Charismatic | Average |
| P01 | Male | ug_high | 67 | Charismatic | Ugly |
| P01 | Male | att_some | 88 | Average | Attractive |
| P01 | Male | av_some | 69 | Average | Average |
| P01 | Male | ug_some | 50 | Average | Ugly |
| P01 | Male | att_none | 97 | Dullard | Attractive |
| P01 | Male | av_none | 48 | Dullard | Average |
| P01 | Male | ug_none | 47 | Dullard | Ugly |
| P02 | Male | att_high | 91 | Charismatic | Attractive |
| P02 | Male | av_high | 83 | Charismatic | Average |
| P02 | Male | ug_high | 53 | Charismatic | Ugly |
| P02 | Male | att_some | 83 | Average | Attractive |
| P02 | Male | av_some | 74 | Average | Average |
| P02 | Male | ug_some | 48 | Average | Ugly |

Boxplots



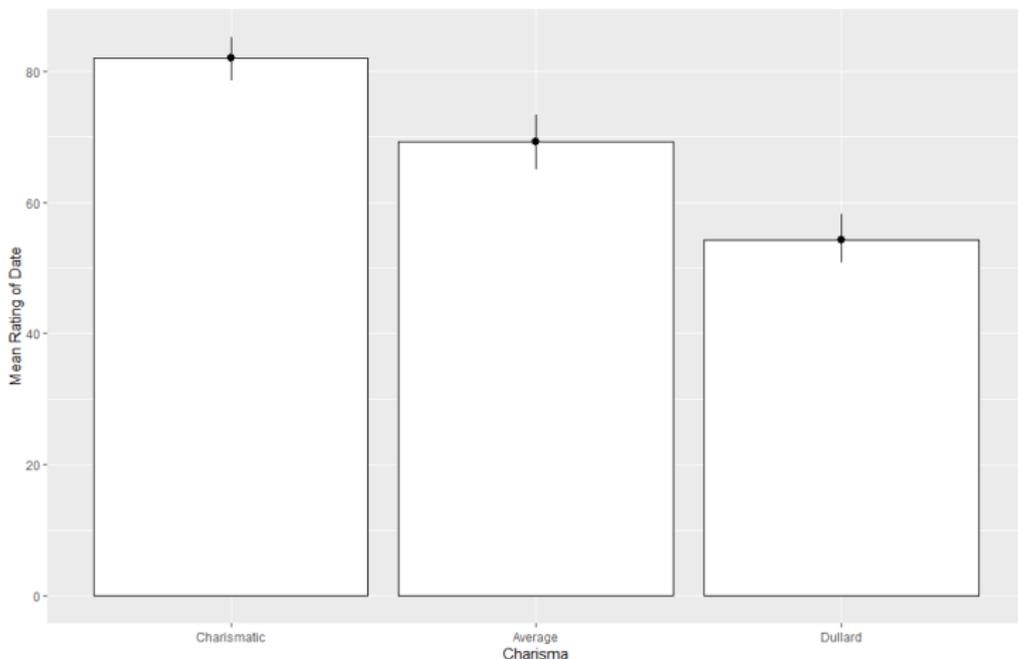
```
dateBoxplot<-ggplot(speedData,aes(looks,dateRating,colour=personality))
dateBoxplot+geom_boxplot()+labs(x="Attractiveness",y="Mean Rating of Date",
  colour="Charisma")+facet_wrap(~gender)
```

Balken Looks



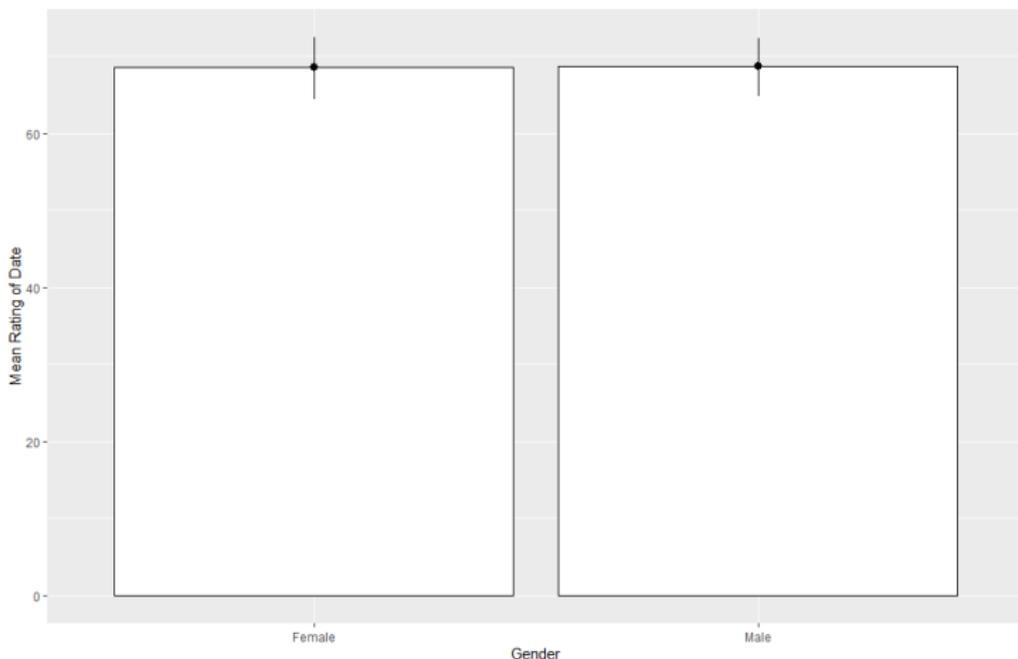
```
looksBar <- ggplot(speedData, aes(looks, dateRating))
looksBar + stat_summary(fun.y = mean, geom = "bar", fill = "White",
  colour = "Black") + stat_summary(fun.data = mean_cl_boot,
  geom = "pointrange") + labs(x = "Attractiveness", y = "Mean Rating of Date")
```

Balken Charisma



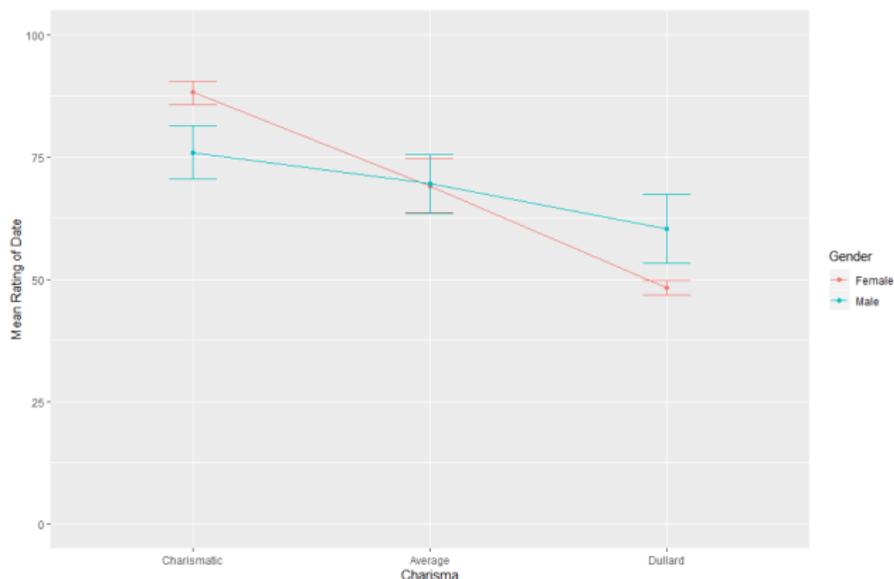
```
charismaBar <- ggplot(speedData, aes(personality, dateRating))
charismaBar + stat_summary(fun.y = mean, geom = "bar", fill = "White",
  colour = "Black") + stat_summary(fun.data = mean_cl_boot,
  geom = "pointrange") + labs(x = "Charisma", y = "Mean Rating of Date")
```

Balken Gender



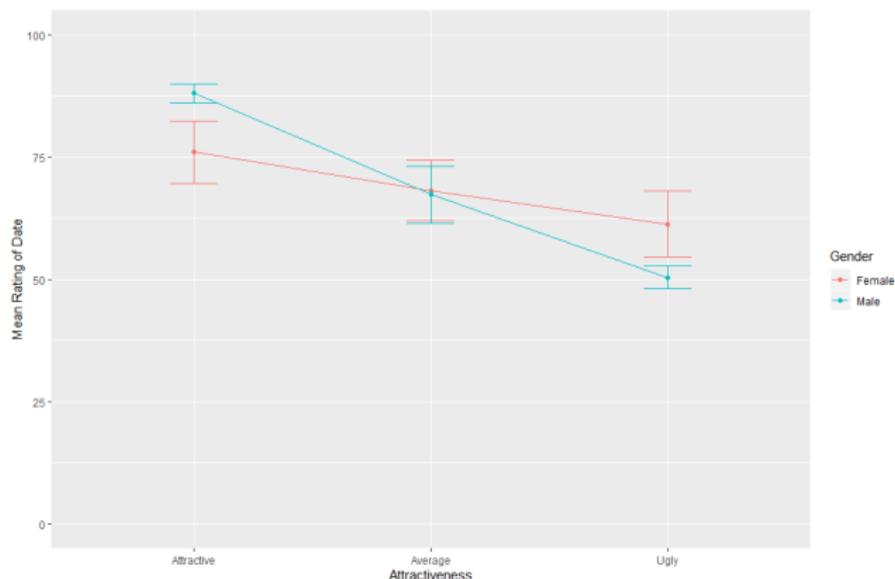
```
genderBar <- ggplot(speedData, aes(gender, dateRating))  
genderBar + stat_summary(fun.y = mean, geom = "bar", fill = "White",  
  colour = "Black") + stat_summary(fun.data = mean_cl_boot,  
  geom = "pointrange") + labs(x = "Gender", y = "Mean Rating of Date")
```

Interaktion Gender Charisma



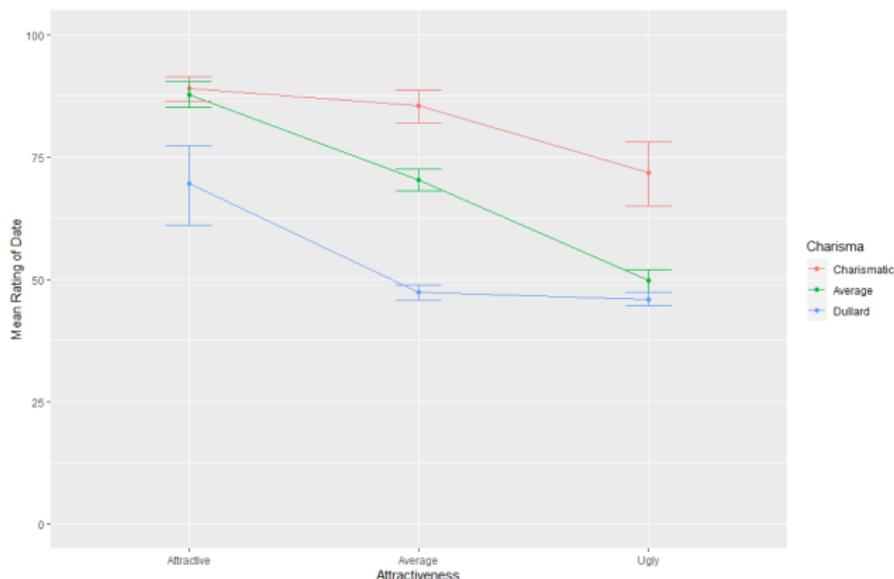
```
genderCharisma <- ggplot(speedData, aes(personality, dateRating,  
  colour = gender))  
genderCharisma + stat_summary(fun.y = mean, geom = "point") +  
  stat_summary(fun.y = mean, geom = "line", aes(group= gender)) +  
  stat_summary(fun.data = mean_cl_boot, geom = "errorbar", width = 0.2) +  
  labs(x = "Charisma", y = "Mean Rating of Date", colour = "Gender") +  
  scale_y_continuous(limits = c(0,100))
```

Interaktion Gender Looks



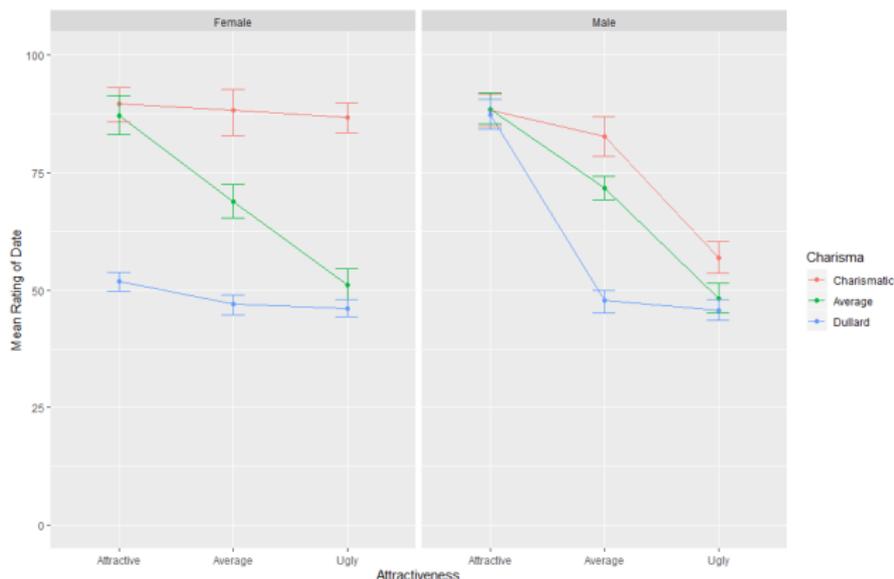
```
genderLooks <- ggplot(speedData, aes(looks, dateRating, colour = gender))
genderLooks + stat_summary(fun.y = mean, geom = "point")
  + stat_summary(fun.y = mean, geom = "line", aes(group= gender))
  + stat_summary(fun.data = mean_cl_boot, geom = "errorbar", width = 0.2)
  + labs(x = "Attractiveness", y = "Mean Rating of Date", colour = "Gender") +
  scale_y_continuous(limits = c(0,100))
```

Interaktion Looks Charisma



```
looksCharisma <- ggplot(speedData, aes(looks, dateRating, colour = personality))
looksCharisma + stat_summary(fun.y = mean, geom = "point")
  + stat_summary(fun.y = mean, geom = "line", aes(group= personality))
  + stat_summary(fun.data = mean_cl_boot, geom = "errorbar", width = 0.2)
  + labs(x = "Attractiveness", y = "Mean Rating of Date", colour = "Charisma")
  + scale_y_continuous(limits = c(0,100))
```

Interaktion Gender Looks Charisma



```
looksCharismaGender <- ggplot(speedData, aes(looks, dateRating, colour = personality))
looksCharismaGender + stat_summary(fun.y = mean, geom = "point")
  + stat_summary(fun.y = mean, geom = "line", aes(group= personality))
  + stat_summary(fun.data = mean_cl_boot, geom = "errorbar", width = 0.2)
  + labs(x = "Attractiveness", y = "Mean Rating of Date", colour = "Charisma")
  + scale_y_continuous(limits = c(0,100)) + facet_wrap(~gender)
```

Überblick

```
by(speedData$dateRating, list(speedData$looks, speedData$personality,  
    speedData$gender), stat.desc, basic = FALSE)
```

```
: Attractive
```

```
: Charismatic
```

```
: Female
```

| median | mean | SE.mean | CI.mean.0.95 | var | std.dev | coef.var |
|-------------|-------------|------------|--------------|-------------|------------|------------|
| 89.00000000 | 89.60000000 | 2.09867683 | 4.74753683 | 44.04444444 | 6.63659886 | 0.07406918 |

```
-----  
: Average
```

```
: Charismatic
```

```
: Female
```

| median | mean | SE.mean | CI.mean.0.95 | var | std.dev | coef.var |
|-------------|-------------|------------|--------------|-------------|------------|------------|
| 90.50000000 | 88.40000000 | 2.63396617 | 5.95844544 | 69.37777778 | 8.32933237 | 0.09422322 |

```
-----  
: Average
```

```
: Dullard
```

```
: Male
```

| median | mean | SE.mean | CI.mean.0.95 | var | std.dev | coef.var |
|-------------|-------------|------------|--------------|-------------|------------|------------|
| 48.00000000 | 47.80000000 | 1.32329555 | 2.99350251 | 17.51111111 | 4.18462795 | 0.08754452 |

```
-----  
: Ugly
```

```
: Dullard
```

```
: Male
```

| median | mean | SE.mean | CI.mean.0.95 | var | std.dev | coef.var |
|-------------|-------------|------------|--------------|-------------|------------|------------|
| 45.50000000 | 45.80000000 | 1.13333333 | 2.56377812 | 12.84444444 | 3.58391468 | 0.07825141 |

```
*Und so weiter*
```

Kontraste

Wir bauen orthogonale Kontraste analog zu vorher

- *ugly* und *dullard* als Kontrollgruppen
- *att vs avg* und *high vs low* als Untersuchungseinheit

| Gruppe | Kontr 1 | Kontr 2 | Gruppe | Kontr 1 | Kontr 2 |
|------------|---------|---------|-------------|---------|---------|
| Attractive | 1 | -1 | Charismatic | 1 | -1 |
| Average | 1 | 1 | Average | 1 | 1 |
| Ugly | -2 | 0 | Dullard | -2 | 0 |

```
SomevsNone<-c(1, 1, -2)
HivsAv<-c(1, -1, 0)
contrasts(speedData$personality)<-cbind(SomevsNone, HivsAv)

AttractivevsUgly<-c(1, 1, -2)
AttractvsAv<-c(1, -1, 0)
contrasts(speedData$looks)<-cbind(AttractivevsUgly, AttractvsAv)
```

Modell berechnen (als ANOVA)

```
options(digits = 3)
speedModel<-ezANOVA(data = speedData, dv = .(dateRating), wid = .(participant),
  between = .(gender), within = .(looks, personality), type = 3, detailed = TRUE)
speedModel
options(digits = 7)
```

| | Effect | DFn | DFd | SSn | SSd | F | p | p<.05 | ges |
|---|--------------------------|-----|-----|----------|------|----------|----------|-------|----------|
| 1 | (Intercept) | 1 | 18 | 846249.8 | 760 | 2.00e+04 | 7.01e-29 | * | 9.94e-01 |
| 2 | gender | 1 | 18 | 0.2 | 760 | 4.74e-03 | 9.46e-01 | | 4.07e-05 |
| 3 | looks | 2 | 36 | 20779.6 | 883 | 4.24e+02 | 9.59e-26 | * | 8.09e-01 |
| 5 | personality | 2 | 36 | 23233.6 | 1274 | 3.28e+02 | 7.69e-24 | * | 8.26e-01 |
| 4 | gender:looks | 2 | 36 | 3944.1 | 883 | 8.04e+01 | 5.23e-14 | * | 4.45e-01 |
| 6 | gender:personality | 2 | 36 | 4420.1 | 1274 | 6.24e+01 | 1.97e-12 | * | 4.74e-01 |
| 7 | looks:personality | 4 | 72 | 4055.3 | 1993 | 3.66e+01 | 1.10e-16 | * | 4.52e-01 |
| 8 | gender:looks:personality | 4 | 72 | 2669.7 | 1993 | 2.41e+01 | 1.11e-12 | * | 3.52e-01 |

\$'Mauchly's Test for Sphericity'

| | Effect | W | p | p<.05 |
|---|--------------------------|-------|-------|-------|
| 3 | looks | 0.960 | 0.708 | |
| 4 | gender:looks | 0.960 | 0.708 | |
| 5 | personality | 0.929 | 0.536 | |
| 6 | gender:personality | 0.929 | 0.536 | |
| 7 | looks:personality | 0.613 | 0.534 | |
| 8 | gender:looks:personality | 0.613 | 0.534 | |

\$'Sphericity Corrections'

| | Effect | GGe | p[GG] | p[GG]<.05 | HFe | p[HF] | p[HF]<.05 |
|---|--------------------------|-------|----------|-----------|-------|----------|-----------|
| 3 | looks | 0.962 | 7.62e-25 | * | 1.074 | 9.59e-26 | * |
| 4 | gender:looks | 0.962 | 1.49e-13 | * | 1.074 | 5.23e-14 | * |
| 5 | personality | 0.934 | 2.06e-22 | * | 1.038 | 7.69e-24 | * |
| 6 | gender:personality | 0.934 | 9.44e-12 | * | 1.038 | 1.97e-12 | * |
| 7 | looks:personality | 0.799 | 9.00e-14 | * | 0.992 | 1.43e-16 | * |
| 8 | gender:looks:personality | 0.799 | 1.47e-10 | * | 0.992 | 1.34e-12 | * |

Modell auswerten

| | Effect | DFn | DFd | SSn | SSd | F | p | p<.05 | ges |
|---|--------------------------|-----|-----|----------|------|----------|----------|-------|----------|
| 1 | (Intercept) | 1 | 18 | 846249.8 | 760 | 2.00e+04 | 7.01e-29 | * | 9.94e-01 |
| 2 | gender | 1 | 18 | 0.2 | 760 | 4.74e-03 | 9.46e-01 | | 4.07e-05 |
| 3 | looks | 2 | 36 | 20779.6 | 883 | 4.24e+02 | 9.59e-26 | * | 8.09e-01 |
| 5 | personality | 2 | 36 | 23233.6 | 1274 | 3.28e+02 | 7.69e-24 | * | 8.26e-01 |
| 4 | gender:looks | 2 | 36 | 3944.1 | 883 | 8.04e+01 | 5.23e-14 | * | 4.45e-01 |
| 6 | gender:personality | 2 | 36 | 4420.1 | 1274 | 6.24e+01 | 1.97e-12 | * | 4.74e-01 |
| 7 | looks:personality | 4 | 72 | 4055.3 | 1993 | 3.66e+01 | 1.10e-16 | * | 4.52e-01 |
| 8 | gender:looks:personality | 4 | 72 | 2669.7 | 1993 | 2.41e+01 | 1.11e-12 | * | 3.52e-01 |

- Mauchly's Test überall nicht signifikant, also Sphärizität gegeben
- Bei *gender* Effekt nicht signifikant → Bei Ignorieren von *personality* und *looks* kein signifikanter Unterschied
- Signifikanter Effekt bei *looks* → Bei Ignorieren von *personality* und *gender* signifikanter Unterschied bei *looks*
- Signifikanter Effekt bei *gender:looks* → Effekt bei *looks* verschieden je nach *gender*
- Signifikanter Effekt bei *gender:looks:personality* → Der signifikante Effekt bei *looks:personality* ist verschieden je nach *gender*
 - Analog bei anderen (und umgekehrten) Kombinationen

Zusammenfassung

- Gemischte ANOVA: Experiment durch Veränderung (mindestens) einer abhängigen und einer unabhängigen Variable
- Schritte
 - 1 Dateneingabe und -Exploration
 - 2 Kontraste erstellen und Modell berechnen
 - 3 Auswerten und ggfalls weitere Auswertung mittels paarweiser t-Tests (gezielt, Kontrastierung) oder per Post Hoc Test (explorativ)
- Übersprungen: Robust (Wilcox, 2005), Gemischtes Design als Lineares Modell/Regression (Siehe Begleitmaterial im Moodle)
- Lineares Modell/Regression flexibler einsetzbar, erlaubt genauere Analysen der Interaktion und kommt ohne Bedingung der Sphärizität aus