

THE STRUCTURE OF WEIGHTED AUTOMATA ON TREES AND TREE-LIKE GRAPHS

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Weighted Feferman-Vaught Theorem

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Büchi-type result for **Quantitative Monitor Automata**

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$$L \text{ recognizable by NFA} \quad \Leftrightarrow \quad L \text{ definable in MSO}$$

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Max-Plus Tree Automata

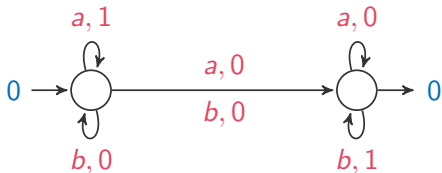
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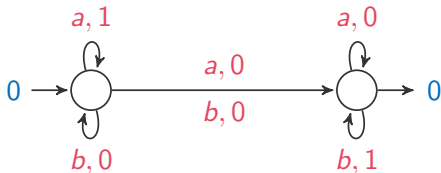
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Equivalence

Unambiguity

(Finite) Sequentiality