

# Multi Bottom-up Tree Transducers

Andreas Maletti

Institute for Natural Language Processing  
Universität Stuttgart, Germany

`maletti@ims.uni-stuttgart.de`

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# Overview

- 1 Motivation
- 2 Extended Multi Bottom-up Tree Transducers
- 3 The Theory
- 4 The Application



# Machine translation

## Translation

- **Input:**  
Official forecasts predicted just 3 percent, Bloomberg said.
- **We:**  
die die offiziellen prognosen nur 3 prozent prognostizierten hat bloomberg gesagt.
- **Google:**  
Offizielle Prognosen vorhergesagt nur 3 Prozent, sagte Bloomberg.



# Machine translation

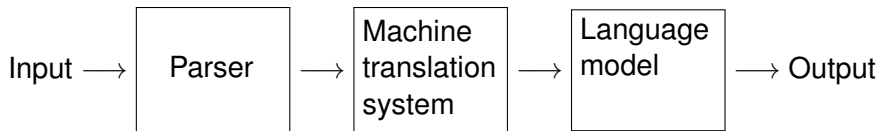
## Translation

- **Input:**  
The ECB wants to hold inflation to under two percent, or somewhere in that vicinity.
- **We:**  
die ezb will unter zwei inflation prozent oder halten irgendwo damit benachbarten gebieten,.
- **Google:**  
Die EZB will die Inflation auf unter zwei Prozent zu halten, oder irgendwo in der Nähe.



# Syntax-based machine translation

## Syntax-based systems



# What do we have?

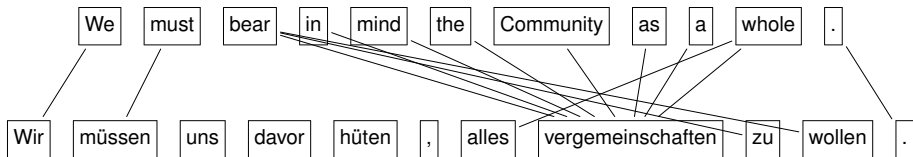
## Input

- parallel text (English and German)
- here: EUROPARL

## Example

- “We must bear in mind the Community as a whole.”
- “Wir müssen uns davor hüten, alles vergemeinschaften zu wollen.”

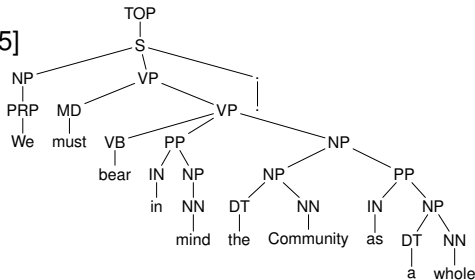
Alignments by GIZA++ [OCH, NEY '03]:



# Parsing

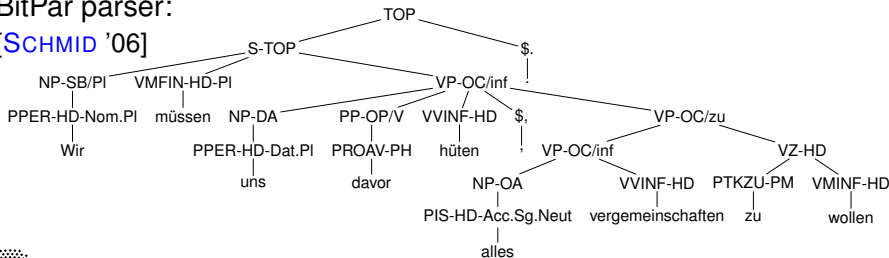
CHARNIAK parser:

[CHARNIAK, JOHNSON '05]



BitPar parser:

[SCHMID '06]

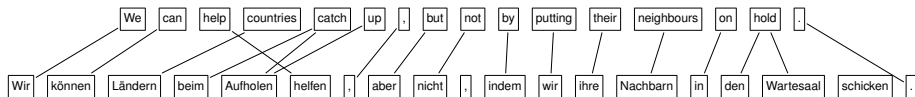


# Better example

## Example

- “We can help countries catch up, but not by putting their neighbours on hold.”
- “Wir können Ländern beim Aufholen helfen, aber nicht, indem wir ihre Nachbarn in den Wartesaal schicken.”

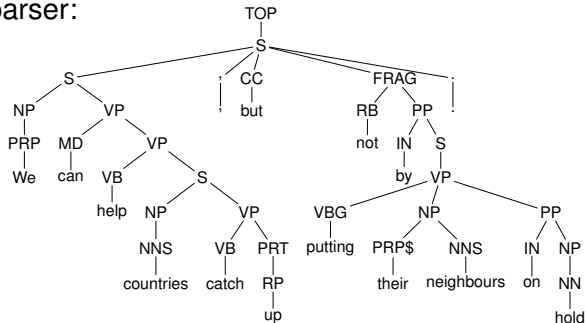
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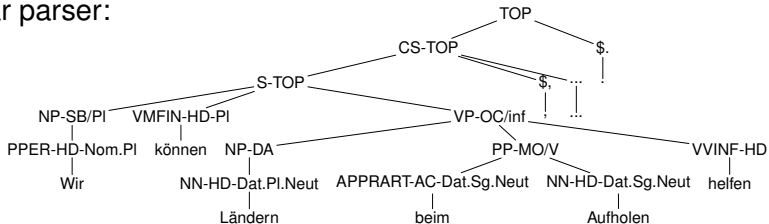


# Better example

CHARNIAK parser:



BitPar parser:



# Small example

## Input

*Yugoslav President Voislav signed for Serbia.*

و تولى التوقيع عن صربيا الرئيس اليوغوسلافي فويسلاف

Transliteration: w twlY AltwqyE En SrbyA Alr}ys AlywgwslAfY fwyslAf.

*And then the matter was decided, and everything was put in place.*

ف كان ان تم الحسم و وضعت الأمور في نصاب ها

Transliteration: f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA.

*Below are the male and female winners in the different categories.*

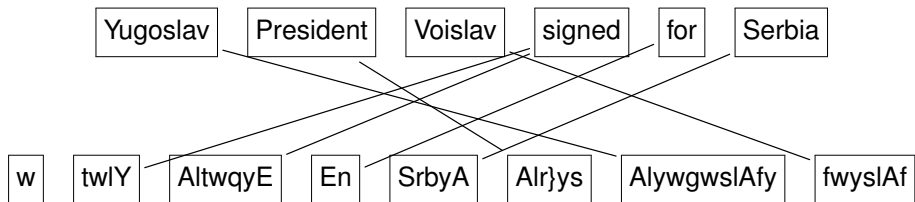
و هنا الأوائل و الأوليات في مختلف الفئات

Transliteration: w hnA Al>wA}l w Al>wlyAt fy mxltf Alf}At.



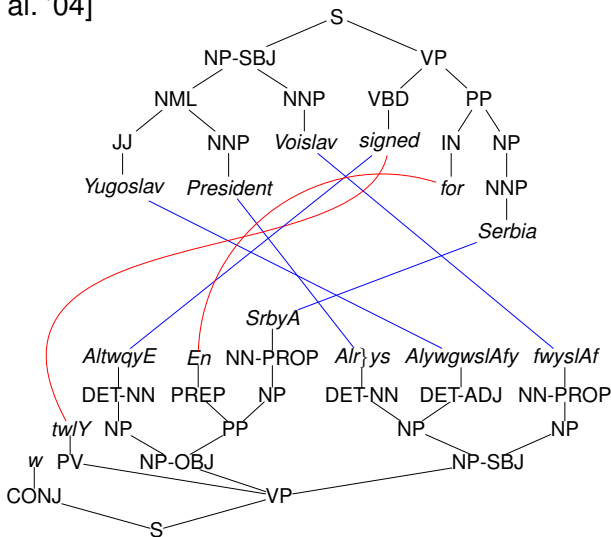
# Small example

## Alignment

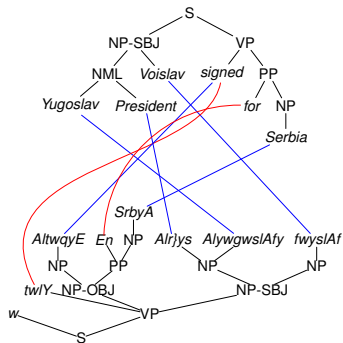


# Rule extraction

[GALLEY et al. '04]



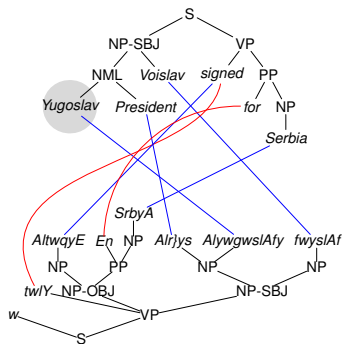
# Rule extraction



- Select next node bottom-up
- Identify maximal subtree of aligned nodes
- Identify subtree of nodes aligned to aligned nodes, etc.
- Extract rule and leave state
- Repeat



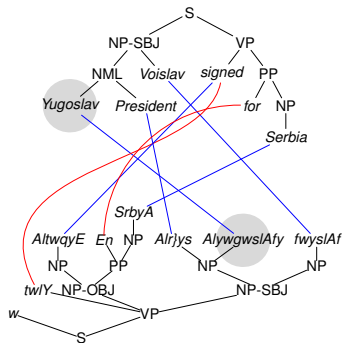
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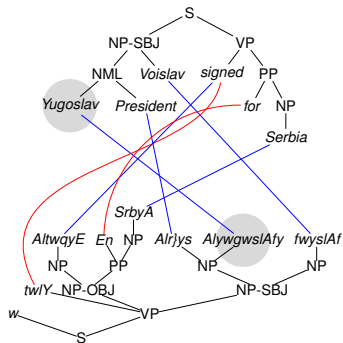
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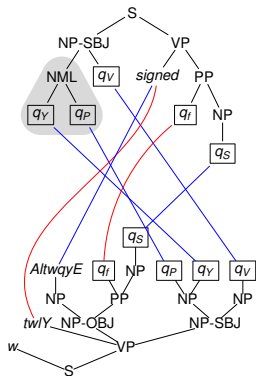








# Rule extraction



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*Yugoslav*  $\xrightarrow{q_Y}$  *AlywqwsIAfy*

*President*  $\xrightarrow{q_P}$  *Alr}ys*

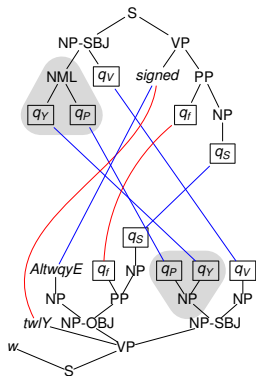
*Voislav*  $\xrightarrow{q_V}$  *fwysIAf*

*for*  $\xrightarrow{q_f}$  *En*

*Serbia*  $\xrightarrow{q_S}$  *SrbyA*



# Rule extraction

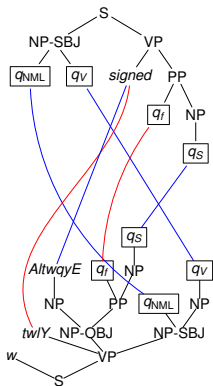


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$$\text{NML}(q_Y, q_P) \xrightarrow{q_{\text{NML}}} \text{NP}(q_P, q_Y)$$



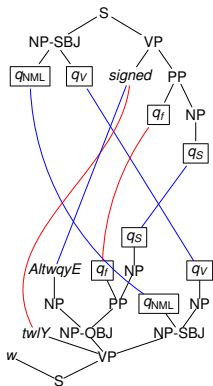
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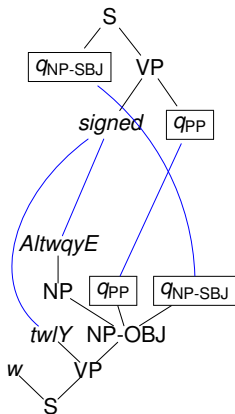
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$$\text{NP-SBJ}(q_{\text{NML}}, q_V) \xrightarrow{q_{\text{NP-SBJ}}} \text{NP-SBJ}(q_{\text{NML}}, \text{NP}(q_V))$$



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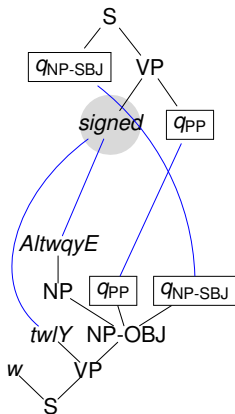
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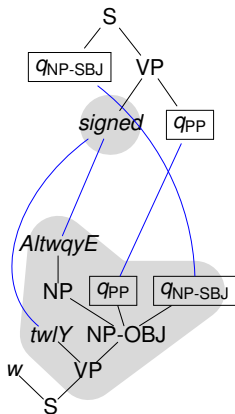
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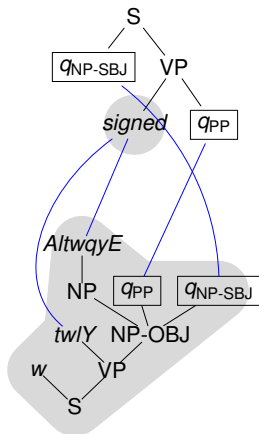
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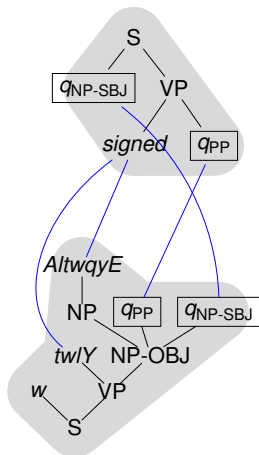
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# Extended top-down tree transducer

## Advantages

- ✓ simple and natural model
- ✓ easy to train (from linguistic resources) [[GRAEHL et al. '08](#)]
- ✓ symmetric

## Implementation

- TIBURON [[MAY, KNIGHT '06](#)]



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# Extended top-down tree transducer

## Disadvantages (also of STSG)

- ✗ no discontinuities
- ✗ not binarizable  
[AHO, ULLMAN '72; ZHANG et al. '06]
- ✗ inefficient input/output restriction  
[M., SATTA '10]
- ✗ not composable  
[ARNOLD, DAUCHET '82]



# Roadmap

- 1 Motivation
- 2 Extended Multi Bottom-up Tree Transducers
- 3 The Theory
- 4 The Application



# Syntax

## Definition

**Extended multi bottom-up tree transducer (XMBOT)**  
system  $(Q, \Sigma, F, R)$

- $Q$  ranked alphabet (states)
- $\Sigma$  ranked alphabet (input/output symbols)
- $F \subseteq Q_1$  (final states)
- $R$  finite set of rules  $\ell \rightarrow r$  (rules)
  - linear  $\ell \in T_{\Sigma}(Q(X))$
  - $r \in Q(T_{\Sigma}(Y))$  with  $Y = \text{var}(\ell)$

## Definition

- **linear** if  $r$  is linear for all  $\ell \rightarrow r \in R$
- **nondeleting** if  $\text{var}(r) = \text{var}(\ell)$  for all  $\ell \rightarrow r \in R$





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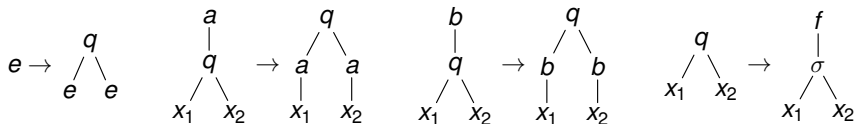


# Syntax

## Example

XMBOT  $(Q, \Sigma, \{f\}, R)$

- $Q = \{q^{(2)}, f^{(1)}\}$
- $\Sigma = \{\sigma^{(2)}, a^{(1)}, b^{(1)}, e^{(0)}\}$
- $R$  contains:



## Note

It is linear and nondeleting

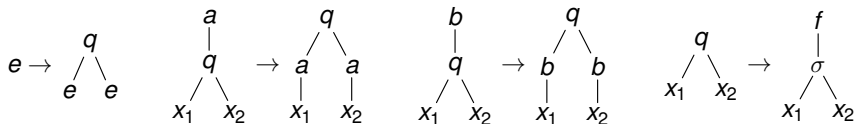


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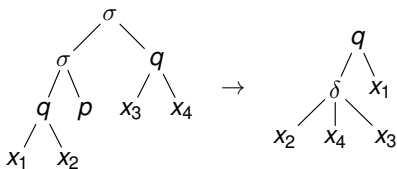
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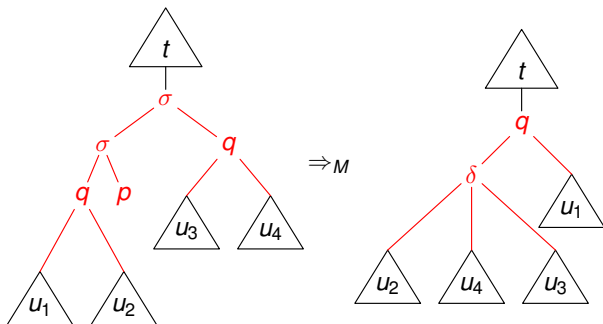


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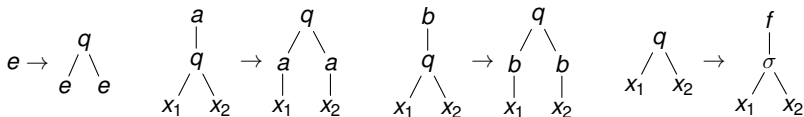
Rule:



Derivation:



# Semantics

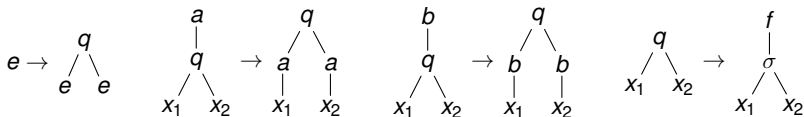


## Example (Derivation)

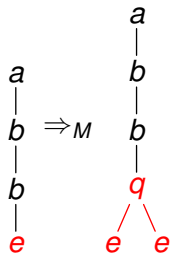
$a$   
 $|$   
 $b$   
 $|$   
 $b$   
 $|$   
 $e$



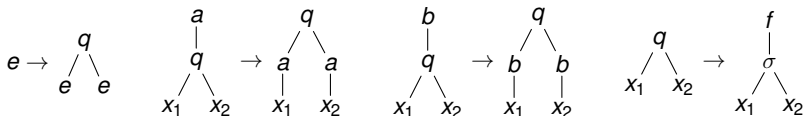
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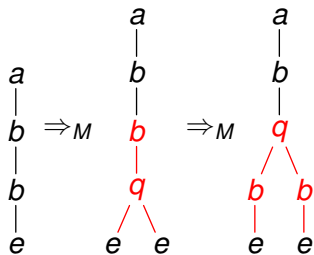
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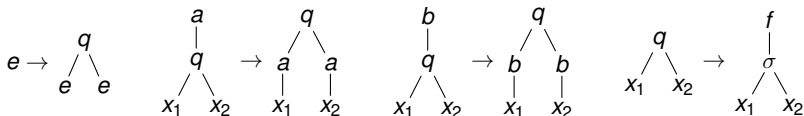
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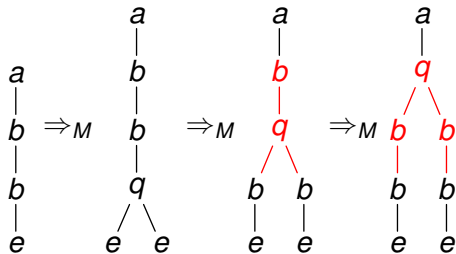
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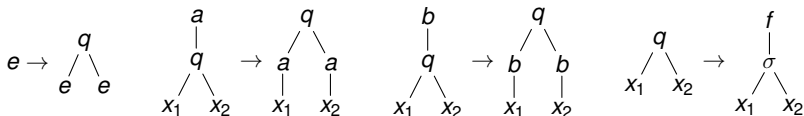


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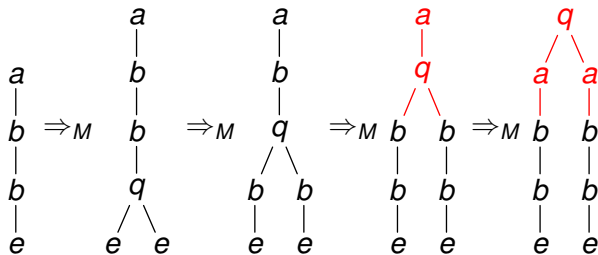




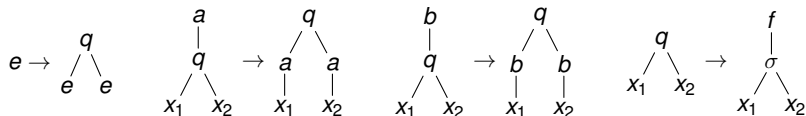
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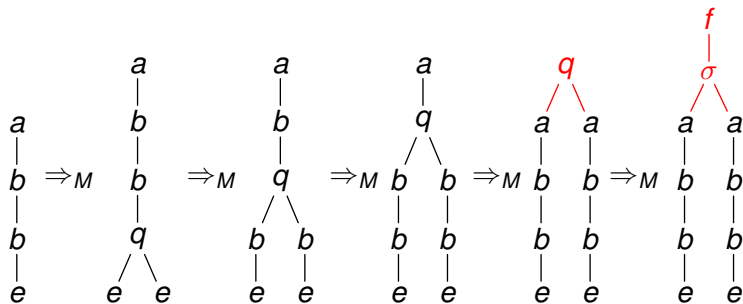
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## Semantics



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# Semantics

## Definition

XMBOT  $M = (Q, \Sigma, F, R)$

$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Sigma \mid \exists q \in F: t \Rightarrow_M^* q(u)\}$$



# Semantics

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## Example

It computes  $\{(t, \begin{matrix} \sigma \\ / \backslash \\ t \quad t \end{matrix}) \mid t \in T_\Sigma\}$

Its image is **not recognizable**



# Restrictions

## Definition

XMBOT  $(Q, \Sigma, F, R)$  is

- **XBOT** if  $Q = Q_1$
- **MBOT** if  $l \in \Sigma(Q(X))$  for all  $l \rightarrow r \in R$



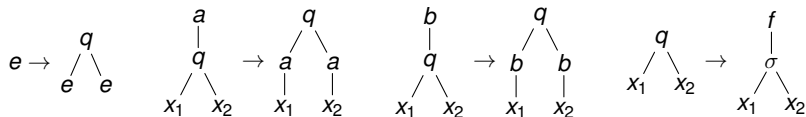
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## Example



It is neither XBOT nor MBOT



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## Proper generalization

Theorem (ENGELFRIET et al. '09)

*All linear XTOP can be simulated by linear XBOT*

Proof.

Standard construction trading input-deletion for output-deletion  
see I-TOP  $\subseteq$  I-BOT by [ENGELFRIET '75] □





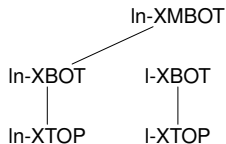
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*All XMBOT can be simulated by nondeleting XMBOT*

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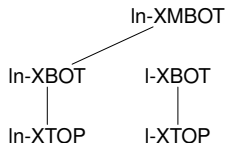
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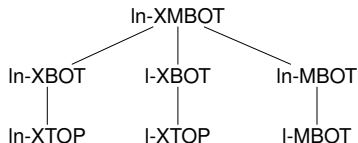
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# Proper generalization

Theorem (ENGELFRIET et al. '09)

*All XMBOT without recursive  $\varepsilon$ -rules can be simulated by MBOT*

Proof.

- Decompose large left-hand sides using “multi”-states
- Attach finite effect of  $\varepsilon$ -rules



# Proper generalization

Theorem (ENGELFRIET et al. '09)

*All XMBOT without recursive  $\varepsilon$ -rules can be simulated by MBOT*

Proof.

- Decompose large left-hand sides using “multi”-states
- Attach finite effect of  $\varepsilon$ -rules



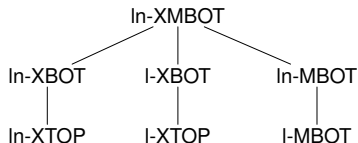
# Proper generalization

Theorem (ENGELFRIET et al. '09)

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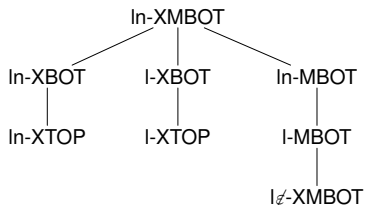
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# Proper generalization

## Definition

- XTOP  $M$  **sensible** if  $|u| \in \mathcal{O}(|t|)$  for all  $(t, u) \in \tau_M$
- **simple** = linear and nondeleting

## Theorem (MALETTI '12)

*All sensible XTOP can be simulated by simple MBOT*

## Proof.

- use (essentially) construction of [ENGELFRIET, MANETH '03]
- obtain finitely copying XTOP (without recursive  $\varepsilon$ -rules)
- apply [ENGELFRIET et al. '09] to obtain linear XMBOT
- previous theorems yield simple MBOT □



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## Corollary

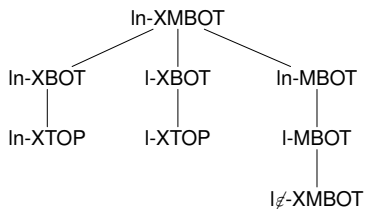
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# Proper generalization

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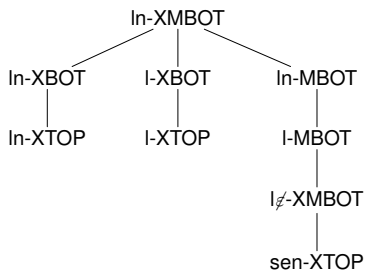
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# Proper generalization

## Theorem

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## Proof.

- even simple MBOT can copy (Example)
- see  $\text{BOT} \not\subseteq \text{TOP}$  by [ENGELFRIET '75]



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*Simple MBOT cannot be weakly simulated by simple XTOP*





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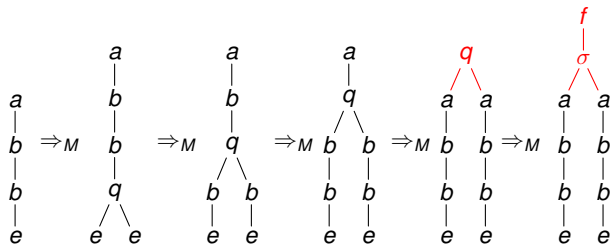
## Summary

- ✓ generalize XTOP (even properly)
- (b) discontinuities
- (c) binarizable
- (d) efficient input/output restriction
- (e) efficiently trainable
- (f) closed under composition



# Discontinuities

## Example (Derivation)



## Discontinuities

- ✗ state covers 1 input subtree
- ✓ state covers several output subtrees

- no input discontinuities
- output discontinuities



## Summary

- ✓ generalize XTOP (even properly)
- ✓ discontinuities (only output side)
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# Binarization

## Definition

XMBOT in **1-symbol normal form**

if exactly 1 (input/output) symbol occurs per rule

Theorem (ENGELFRIET et al. '09)

*All XMBOT can be simulated by 1-symbol normal form XMBOT*



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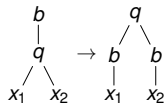
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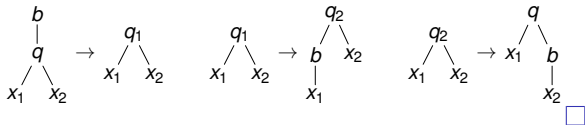
*All XMBOT can be simulated by 1-symbol normal form XMBOT*

Proof.

Original rule:



Replacement rules:





# Binarization

## Definition

XMBOT is **fully binarized** if  $\leq 3$  states per rule  
( $\leq 2$  in left-hand side)

## Theorem (M. '11)

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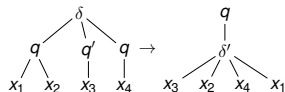
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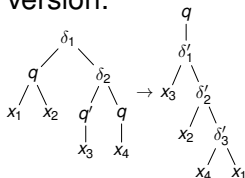
*All XMBOT can be fully binarized (in linear time)*

Proof (Binarize trees and transform into 1-symbol normal form).

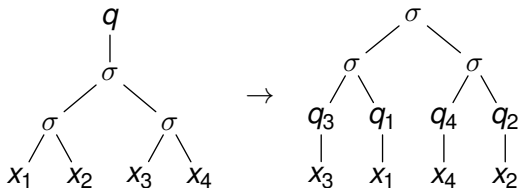
Original rule:



Binarized version:



# Binarization



## Comparison

STSG cannot be binarized, but people try ...

- [ZHANG et al. '06]
- [DENERO et al. '09]



## Corollary

*All XMBOT can be transformed (in linear time)  
from joint to conditional distribution*

## Summary

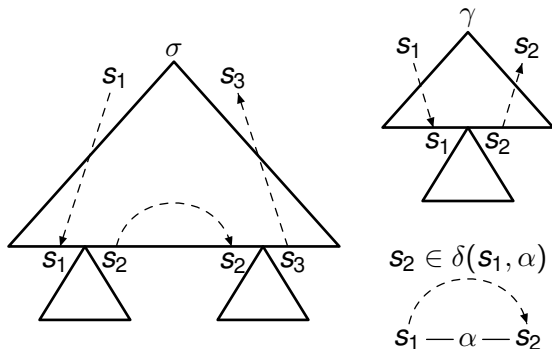
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- ✓ discontinuities (only output side)
- ✓ binarizable
- (d) efficient input/output restriction
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# Input/output restriction

## Definition

**Input restriction** restricts the string language of the domain of an XMBOT to a regular language



# Input/output restriction

Theorem (M., SATTA '10 & M. '11)

Restricting the ... by FSA  $A$  is ...

<i>device</i>	<i>input</i>	<i>output</i>
<i>linear XMBOT</i> $M$	$\mathcal{O}( M  \cdot  A ^3)$	$\mathcal{O}( M  \cdot  A ^x)$
<i>simple XTOP</i> $M$	$\mathcal{O}( M  \cdot  A ^y)$	$\mathcal{O}( M  \cdot  A ^y)$

with  $x = 2 \operatorname{rk}(M) + 2$  and  $y = 2 \operatorname{rk}(M) + 5$



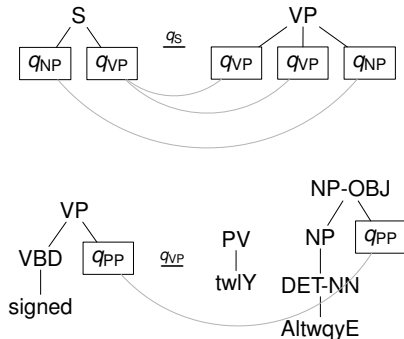
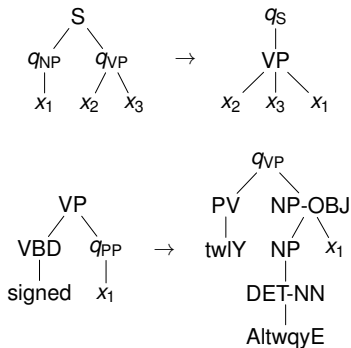
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## A top-down variant



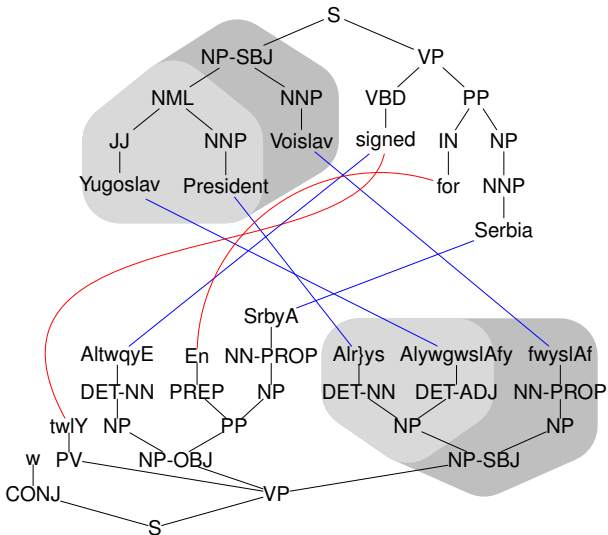
[M. '11]



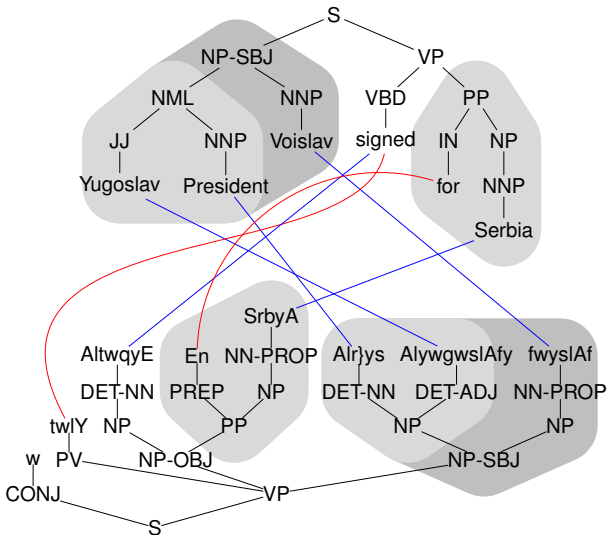




## Rule extraction

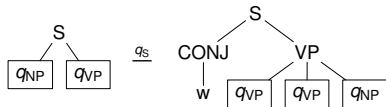
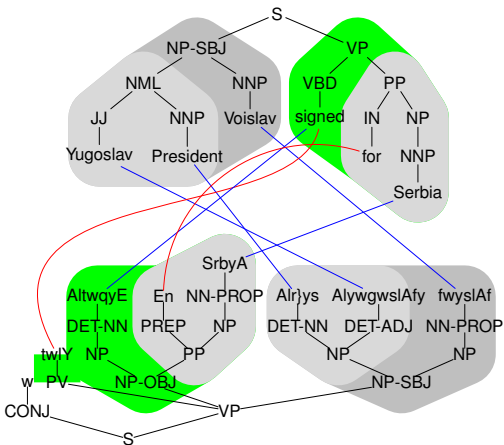


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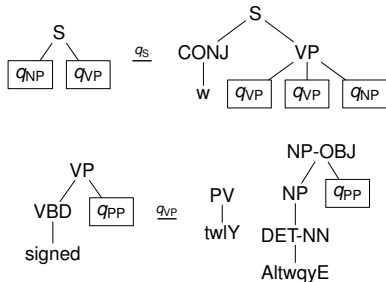
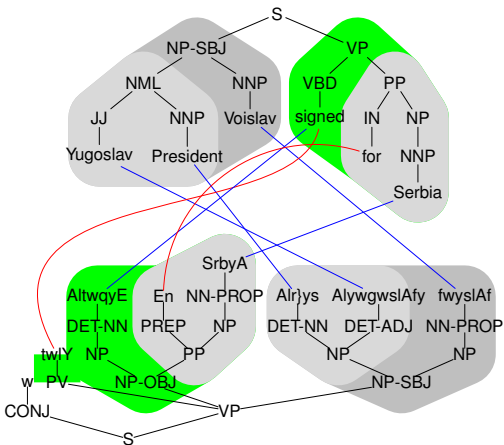




# Rule extraction



# Rule extraction





# EM training

## Theorem

*Derivations of XMBOT are **regular** (even in the weighted case)*

## Conclusion

program of [GRAEHL et al '08] works

- given translation pair  $(s_1, s_2)$
- input- and output restrict to  $s_1$  and  $s_2$
- build derivations
- compute relative “usefulness” of each rule
- move to the next training sentence (and start anew)



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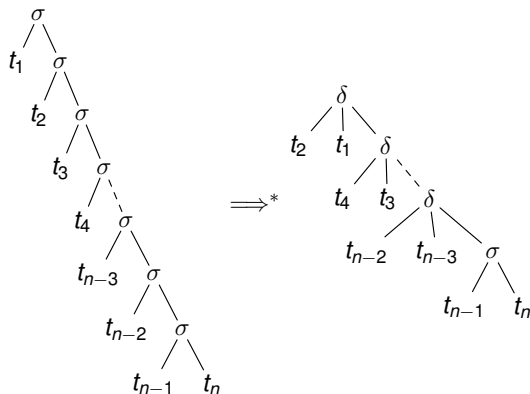


## Summary

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- (f) closed under composition



# Composition of STSG

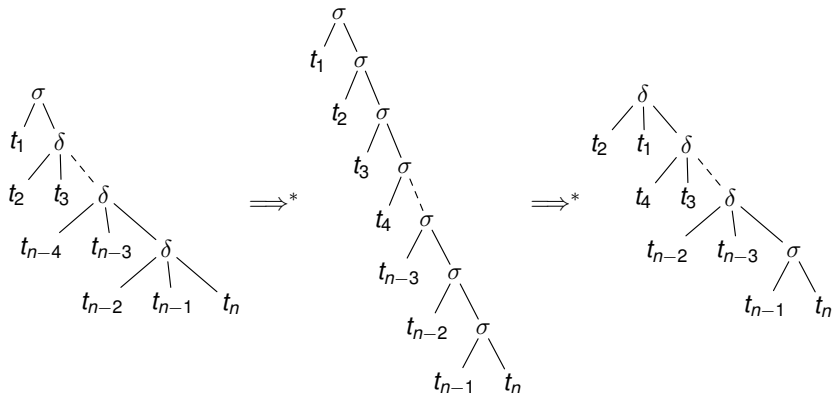


Conclusion

STSGs are not composable!



# Composition of STSG

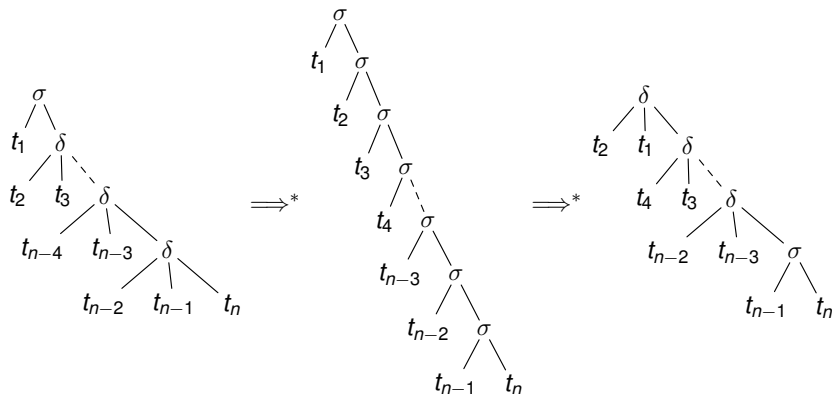


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# Composition of STSG



## Conclusion

STSGs are not composable!



## Composition of XTOP

restrictions	closed?	level of closure
simple, non-erasing, $\varepsilon$ -free	X	2
simple, non-erasing	X	$\infty$
simple, $\varepsilon$ -free	X	$\infty$
simple	X	$\infty$
linear	X	$\geq 2$
linear with regular look-ahead	X	$\geq 2$
general	X	$\infty$



# Composition of XMBOT

restrictions	closed?	level of closure
simple	✓	1
linear	✓	1
general	✗	$\infty$ (?)





# Composition construction

## Definition

XMBOT  $M = (Q, \Sigma, F, R)$  and  $N = (Q', \Sigma, G, R')$   
in 1-symbol normal form

$$M ; N = (Q(Q'), \Sigma, F(G), R'')$$

with

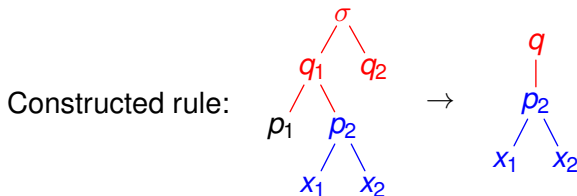
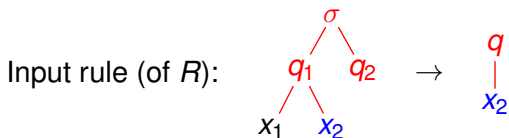
- 1 input-consuming rules from input-consuming rules of  $R$
- 2  $\varepsilon$ -rules from  $\varepsilon$ -rules of  $R'$
- 3  $\varepsilon$ -rules from  $\varepsilon$ -rule of  $R$  followed by input consuming rule of  $R'$



# Composition construction

## Example

(1) Input-consuming rule of  $R$  and resulting rule:



# Composition construction

## Example

(2)  $\varepsilon$ -rule of  $R'$  and resulting rule:

Input rule (of  $R'$ ):  $p_1 \rightarrow \begin{array}{c} p \\ | \\ \alpha \end{array}$

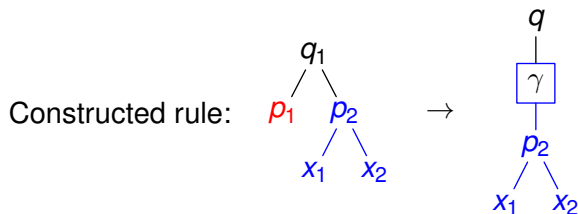
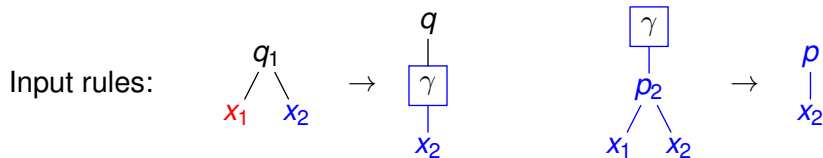
Constructed rule:  $\begin{array}{c} q_1 \\ / \quad \backslash \\ p_1 \quad p_2 \\ | \quad / \quad \backslash \\ x_1 \quad x_1 \quad x_2 \end{array} \rightarrow \begin{array}{c} q_1 \\ / \quad \backslash \\ p \quad p_2 \\ | \quad / \quad \backslash \\ \alpha \quad x_1 \quad x_2 \end{array}$



# Composition construction

## Example

(3)  $\varepsilon$ -rule of  $R$  and input-consuming of  $R'$  and resulting rule:



# Composition construction

Theorem (ENGELFRIET et al. '09)

*The standard bottom-up tree transducer composition results hold*

## Summary

- ✓ generalize XTOP (even properly)
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- ✓ binarizable
- ✓ efficient input/output restriction (less efficient for output)
- ✓ efficiently trainable (messy for permissive MBOT)
- ✓ closed under composition (standard bottom-up results)



# Summary

- ✓ generalize XTOP
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- ✓ preserve regularity backward
- ✗ preserve regularity forward
- ✗ symmetric





# Overview

- 1 Motivation
- 2 Extended Multi Bottom-up Tree Transducers
- 3 The Theory
- 4 The Application**



# XMBOT in machine translation

Moses [KOEHN et al. '07]

- framework for statistical MT
- implementations for many standard tasks (alignment, lexical scores, language model, BLEU scoring)
- supports syntax-based MT

We added

- XMBOT rule support
- XMBOT chart decoder
- adjusted language model calls



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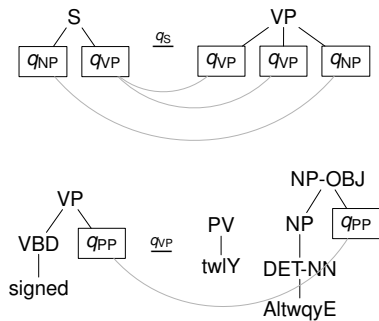
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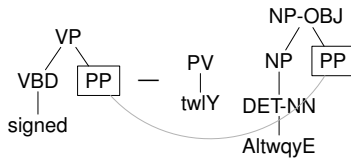
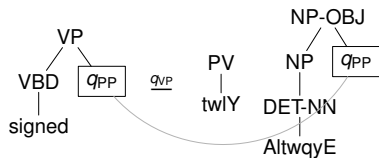
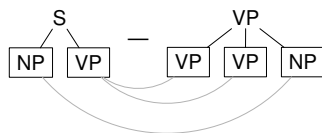
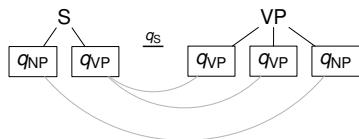
- XMBOT rule support
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- adjusted language model calls (still broken)



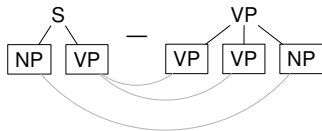
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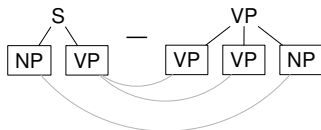
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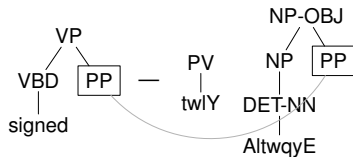
S (NP, VP) ||| VP (VP, VP, NP) ||| S ||| VP ||| 0-2 1-0 1-1 ||| ...



# XMBOT rule encoding



S (NP,VP) ||| VP (VP,VP,NP) ||| S ||| VP ||| 0-2 1-0 1-1 ||| ...



VP (VBD(signed),PP) ||| PV (twIY) || NP-OBJ (NP (DET-NN (AltwqyE)), PP) |||

VP ||| PV NP-OBJ ||| || 0-0 ||| ...





# XMBOT decoder

## FABIENNE BRAUNE

- CYK-like chart parser
- only forward application (backward planned)
- supports all standard features
- integrated cube pruning with language model

## Notes

- reasonably fast
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- we are still working on it



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## NINA SEEMANN

- rule extraction
- input/output restriction
- EM training
- conversion tools, pipeline scripts, ...

## Notes

- in PYTHON (not inside MOSES)
- computationally quite expensive
- variants for reduced POS-tags



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# References

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