

Tree Transducers in Machine Translation

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Machine translation

Applications

- **Technical manuals**

Example (An mp3 player)

The synchronous manifestation of lyrics is a procedure for can broadcasting the music, waiting the mp3 file at the same time showing the lyrics.

With the this kind method that the equipments that synchronous function of support up broadcast to make use of document create setup, you can pass the LCD window way the check at the document contents that broadcast.

That procedure returns offerings to have to modify, and delete, and stick top , keep etc. edit function.

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Machine translation

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- **TripAdvisor**[®]

Example (Hotel Uppsala, Sweden)

Wir hatten die Zimmer eingestuft wird als "Superior" weil sie renoviert wurde im letzten Jahr oder zwei. Unsere Zimmer hatten Parkettboden und waren sehr geräumig. Man musste allerdings nicht musste seitwärts bewegen.

Machine translation

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Example (Hotel Uppsala, Sweden)

Nos alojamos en habitaciones clasificado como “superior” porque se lo habían renovado en el año pasado o dos. Nuestras habitaciones tenían suelos de madera y eran espaciosas. No te tenías que caminar arriba para movernos por allí.

Machine translation

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Example (Hotel Uppsala, Sweden)

Wir hatten die Zimmer eingestuft wird als “Superior” weil sie renoviert wurde im letzten Jahr oder zwei. Unsere Zimmer hatten Parkettboden und waren sehr geräumig. Man musste allerdings nicht musste seitwärts bewegen.

— *We stayed in rooms classified as “superior” because they had been renovated in the last year or two. Our rooms had wood floors and were roomy. You didn’t have to walk sideways to move around.*

Machine translation

Applications

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- TripAdvisor[®]
- **Military**

Example (JONES, SHEN, HERZOG 2009)

Soldier: Okay, what is your name?

Local: Abdul.

Soldier: And your last name?

Local: Al Farran.

Machine translation

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Speech-to-text machine translation

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Local: milk a mechanic and I am here
I mean yes

Machine translation

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Speech-to-text machine translation

Soldier: Okay, what's your name?

Local: milk a mechanic and I am here
I mean yes

Soldier: What is your last name?

Local: every two weeks
my son's name is ismail

Machine translation

Applications

- Technical manuals
- TripAdvisor[®]
- Military
- MSDN, Knowledge Base
- ...

Machine translation (cont'd)

Systems

- GOOGLE translate translate.google.com
- BING translator www.microsofttranslator.com
- LANGUAGE WEAVER + SDL www.freetranslation.com
- ...

Machine translation (cont'd)

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Try them!

Machine translation (cont'd)

History

1 Dark age (60s–90s)

- ▶ rule-based systems (e.g., SYSTRAN)
- ▶ CHOMSKYAN approach
- ▶ perfect translation, poor coverage

2 Reformation (1991–present)

- ▶ word-based, phrase-based, syntax-based systems
- ▶ statistical approach
- ▶ cheap, automatically trained

3 Potential future

- ▶ semantics-based systems (e.g., FRAMENET)
- ▶ semi-supervised, statistical approach
- ▶ basic understanding of translated text

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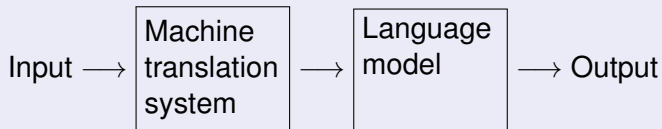
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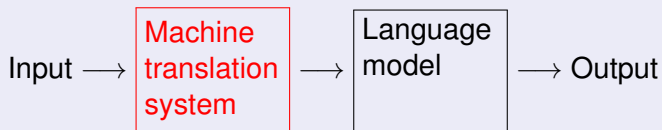
Machine translation (cont'd)

Schema



Machine translation (cont'd)

Schema



Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الحسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

And then the matter was decided , and everything was put in place

Output:

Word-based system (FST)

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<i>f</i>	<i>kAn</i>	<i>An</i>	<i>tm</i>	<i>AlHsm</i>	<i>w</i>	<i>wDEt</i>	<i>Al>mwr</i>	<i>fy</i>	<i>nSAb</i>	<i>hA</i>

Derivation

Input:

the matter was decided , and everything was put in place

Output:

Word-based system (FST)

And then the matter was decided , and everything was put in place

ها نصاب في الأمور وضعت و الحسم تم ان كان ف
hA nSAb fy Al>mwr wDEt w AlHsm tm An kAn f

Derivation

Input:

the matter was decided , and everything was put in place

Output:

f

Word-based system (FST)

And then the matter was decided , and everything was put in place

ها نصاب في الأمور وضعت و تم الحسم ان كان ف
hA nSAb fy Al>mwr wDEt w tm AlHsm An kAn f

Derivation

Input:

the matter was decided , and everything was put in place

Output:

f kAn

Word-based system (FST)

And then the matter was decided , and everything was put in place

كان ان تم الحسم و وضعت الامور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

the matter *was decided , and everything was put in place*

Output:

f kAn

Word-based system (FST)

And then the matter was decided , and everything was put in place

كان ان تم الحسم و وضعت الامور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

the matter was *decided , and everything was put in place*

Output:

f kAn

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الحسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

*the matter was **decided** , and everything was put in place*

Output:

f kAn

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الجسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

the matter *, and everything was put in place*

Output:

f kAn An tm AlHsm

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الحسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

the matter and *everything was put in place*

Output:

f kAn An tm AlHsm

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الجسم و وضعت الامور في نصاب ها
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Derivation

Input:

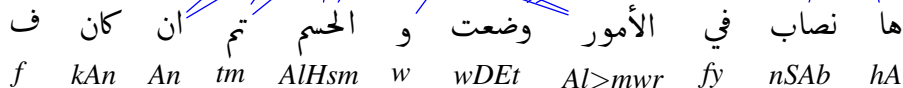
the matter everything *was put in place*

Output:

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Word-based system (FST)

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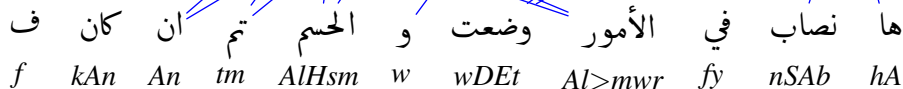
the matter was *put in place*

Output:

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Word-based system (FST)

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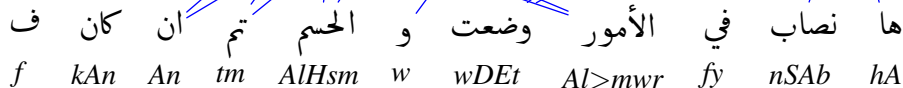
the matter was put in place

Output:

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And then the matter was decided , and everything was put in place



ف كان ان تم الحسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

the matter in *place*

Output:

f kAn An tm AlHsm w wDEt

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف	كان	ان	تم	الحسم	و	وضعت	الأمر	في	نصاب	ها
<i>f</i>	<i>kAn</i>	<i>An</i>	<i>tm</i>	<i>AlHsm</i>	<i>w</i>	<i>wDEt</i>	<i>Al>mwr</i>	<i>fy</i>	<i>nSAb</i>	<i>hA</i>

Derivation

Input:

in place

Output:

f kAn An tm AlHsm w wDEt Al>mwr

Word-based system (FST)

And then the matter was decided , and everything was put in place

ها نصاب في الأمور وضعت و تم الحسم ان كان ف
hA nSAb fy Al>mwr wDEt w tm AlHsm An kAn f

Derivation

Input:

place

Output:

f kAn An tm AlHsm w wDEt Al>mwr fy

Word-based system (FST)

And then the matter was decided , and everything was put in place

ف كان ان تم الجسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

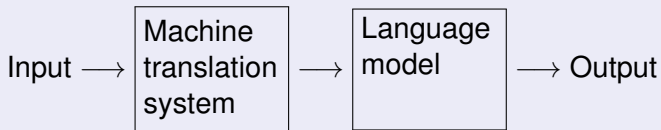
□

Output:

f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Phrase-based machine translation

Schema

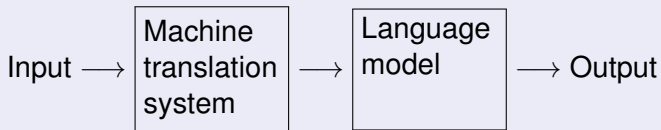


Phrase-based systems

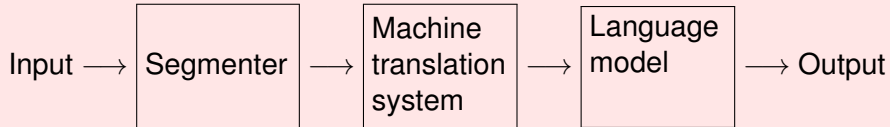


Phrase-based machine translation

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Phrase-based systems



Phrase-based system (FST+Perm)

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Derivation

Input:

And then the matter was decided , and everything was put in place

Output:

Phrase-based system (FST+Perm)

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ف كان ان تم الحسم و وضعت الأمور في نصاب ها
f kAn An tm AlHsm w wDEt Al>mwr fy nSAb hA

Derivation

Input:

*And then*₁ *the matter*₅ *was decided*₂ *, and everything*₃ *was put*₄ *in place*₆

Output:

Phrase-based system (FST+Perm)

And then the matter was decided , and everything was put in place

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Derivation

Input:

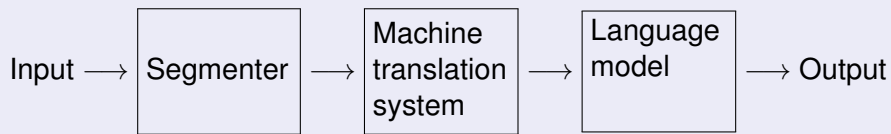
*And then*₁ *the matter*₅ *was decided*₂ *, and everything*₃ *was put*₄ *in place*₆

Output:

*f kAn*₁ *An tm AlHsm*₂ *w*₃ *wDEt*₄ *Almwr*₅ *fy nSAb hA*₆

Machine translation (cont'd)

Phrase-based systems

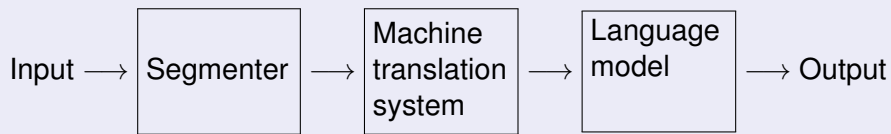


Syntax-based systems

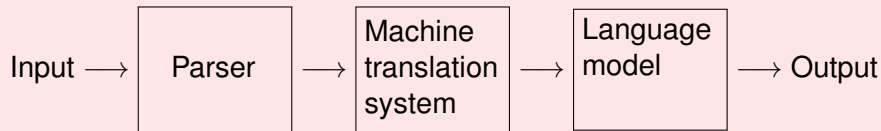


Machine translation (cont'd)

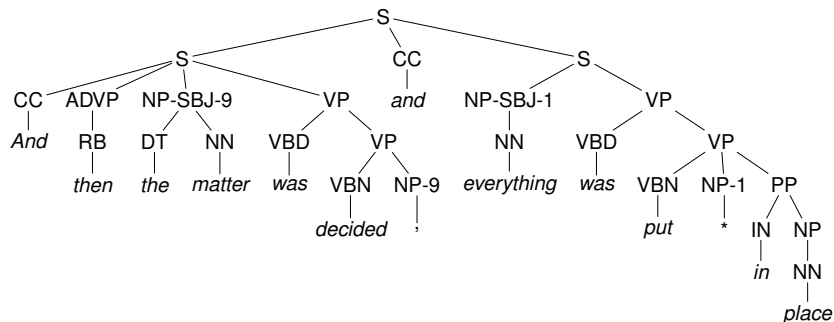
Phrase-based systems



Syntax-based systems

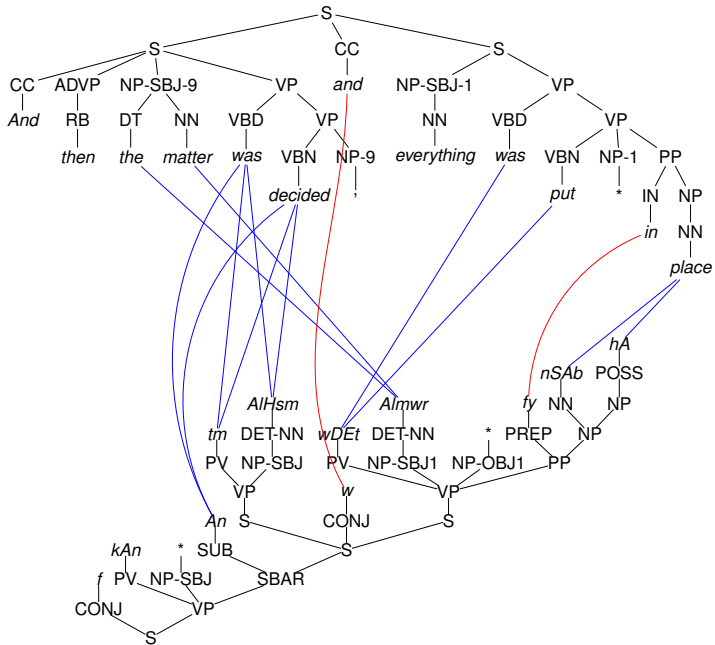


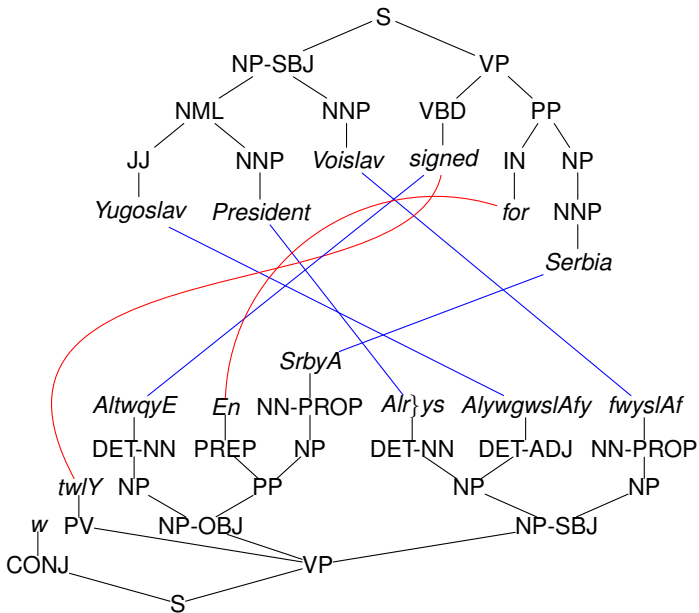
Parser



And then the matter was decided , and everything was put in place

(thanks to [KEVIN KNIGHT](#) for the data)





Contents

- 1 Machine Translation
- 2 Extended Top-down Tree Transducers
- 3 Multi Bottom-up Tree Transducers
- 4 Synchronous Tree-Adjoining Grammars

Weight structure

Definition

Commutative semiring $(C, +, \cdot, 0, 1)$ if

- $(C, +, 0)$ and $(C, \cdot, 1)$ commutative monoids
- \cdot distributes over finite (incl. empty) sums

Example

- BOOLEAN semiring $(\{0, 1\}, \max, \min, 0, 1)$
- Semiring $(\mathbb{R}_{\geq 0}, +, \cdot, 0, 1)$ of probabilities
- Tropical semiring $(\mathbb{N} \cup \{\infty\}, \min, +, \infty, 0)$
- Any field, ring, etc.

Most of the talk: BOOLEAN semiring

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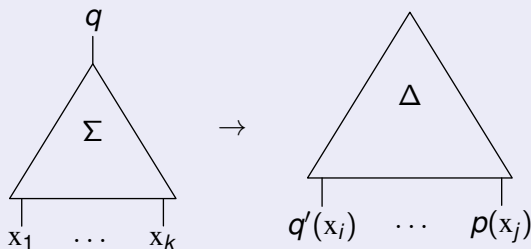
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Most of the talk: BOOLEAN semiring

Syntax

Definition (ARNOLD, DAUCHET 1976, GRAEHL, KNIGHT 2004)

Extended top-down tree transducer (XTOP) $M = (Q, \Sigma, \Delta, l, R)$
with finitely many rules

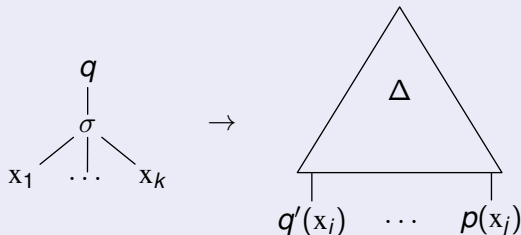


- $q, q', p \in Q$ are states
- $i, j \in \{1, \dots, k\}$

Syntax (cont'd)

Definition (ROUNDS 1970, THATCHER 1970)

- **Top-down tree transducer** (TOP) if all rules

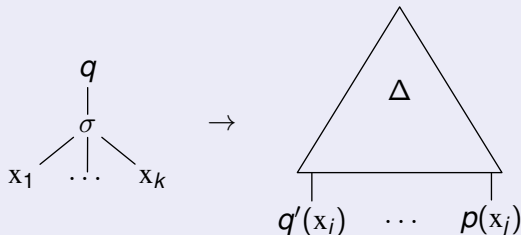


- **linear** if no variable occurs twice in r for all rules $l \rightarrow r$
- **nondeleting** if $\text{var}(l) = \text{var}(r)$ for all rules $l \rightarrow r$

Syntax (cont'd)

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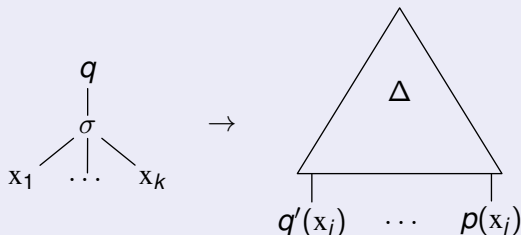


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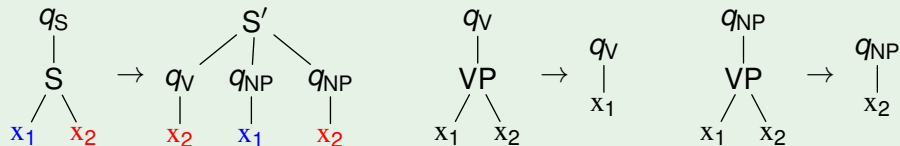


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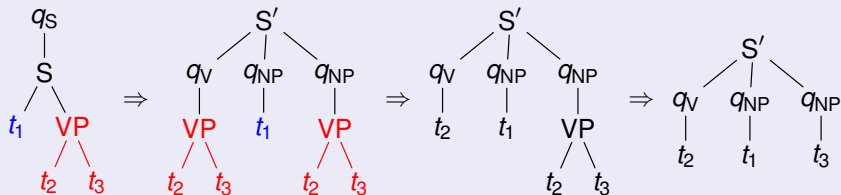
Semantics

Example

States $\{q_S, q_V, q_{NP}\}$ of which only q_S is initial



Derivation

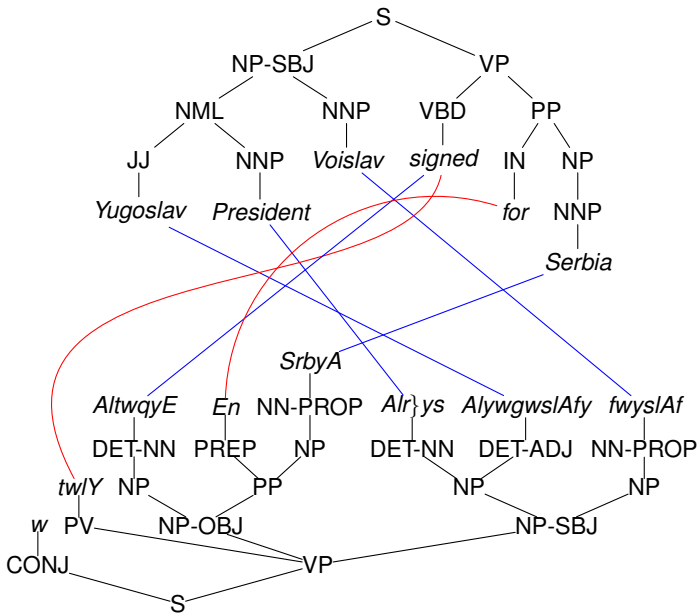


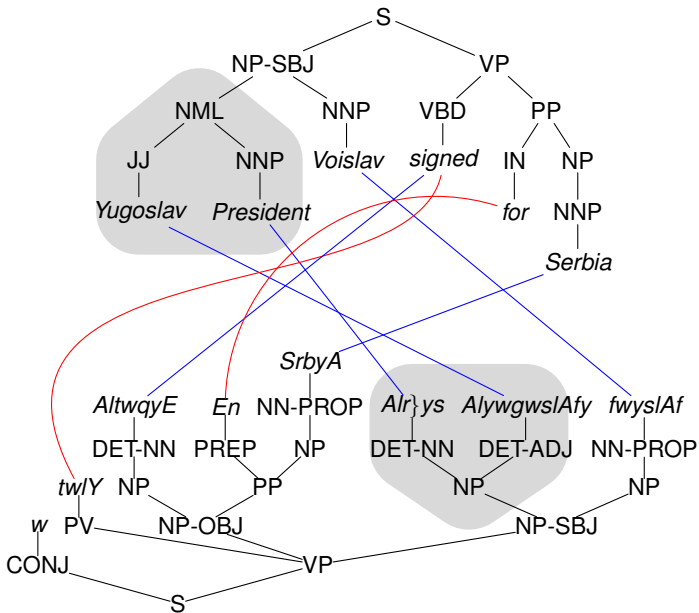
Semantics (cont'd)

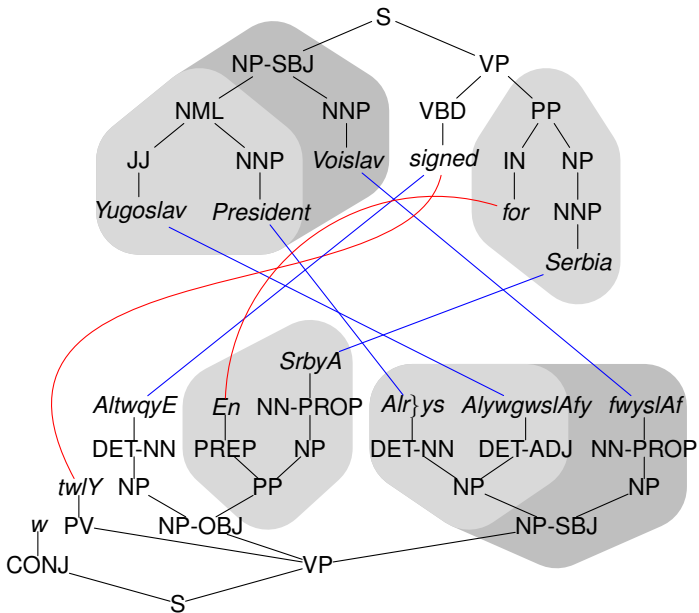
Definition

Computed transformation:

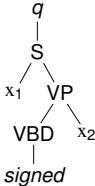
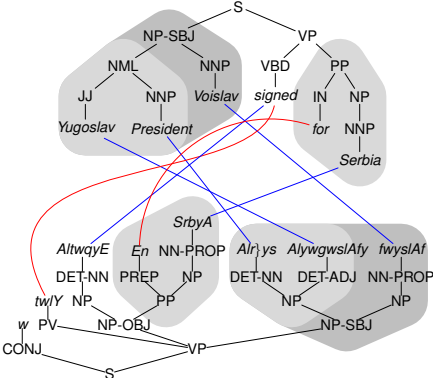
$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in I: q(t) \Rightarrow^* u\}$$



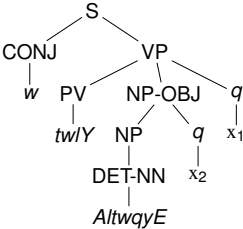




Rule extraction

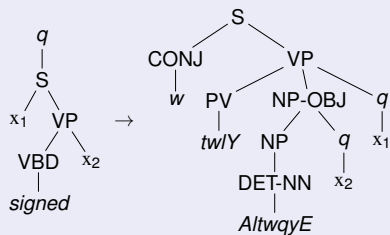


→



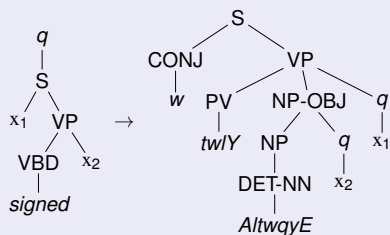
Symmetry

Original rule

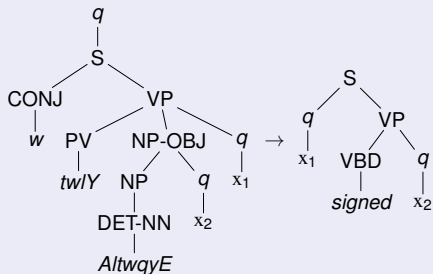


Symmetry

Original rule

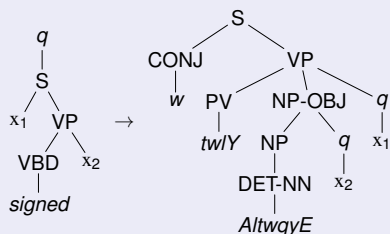


Inverted rule

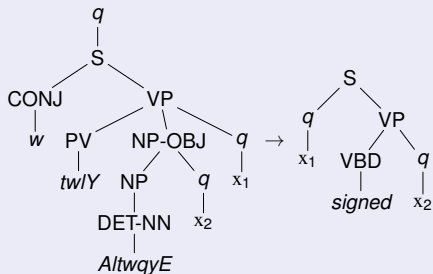


Symmetry

Original rule



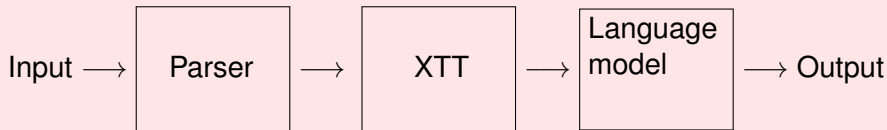
Inverted rule



Linear nondeleting XTT can be inverted

Preservation of regularity

Schematics



Parse trees

- best parse tree
- n -best parses
- all parses

Can all be represented by **regular** tree language

Preservation of regularity

Schematics



Parse trees

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Can all be represented by **regular** tree language

Preservation of regularity (cont'd)

Schematics



Approach

- Input restriction
- Project to output

Result

Linear XTT preserve regularity

Preservation of regularity (cont'd)

Schematics



Approach

- Input restriction
- Project to output

Result

Linear XTT preserve regularity

Preservation of regularity (cont'd)

Schematics



Approach

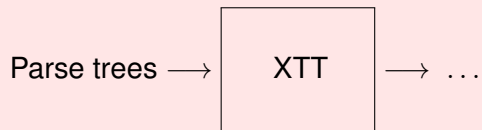
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Linear XTT preserve regularity

Composition

Schematics

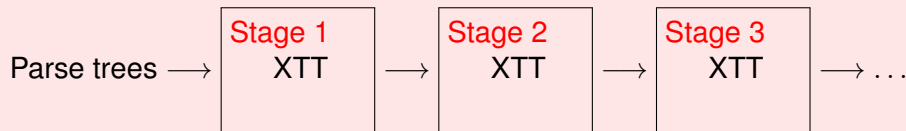


Example (YAMADA, KNIGHT 2002)

- Reorder
- Insert words
- Translate words

Composition

Schematics

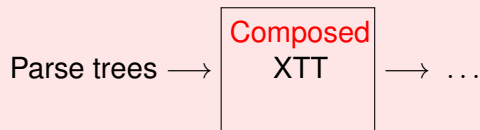


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Schematics

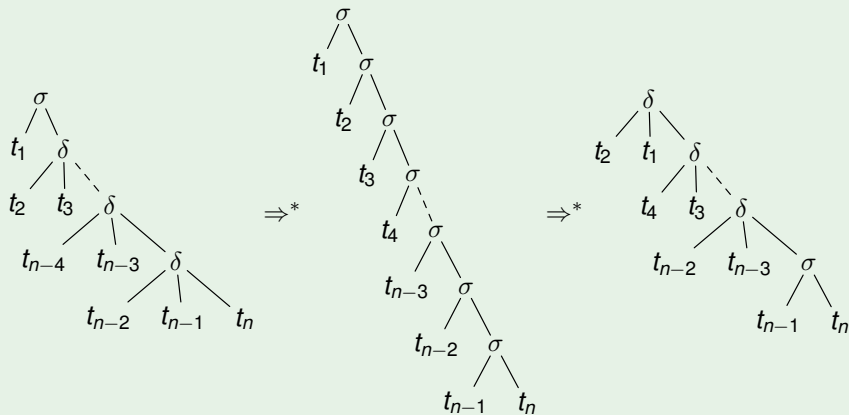


Example (YAMADA, KNIGHT 2002)

- Reorder
- Insert words
- Translate words

Composition (cont'd)

Example (ARNOLD, DAUCHET 1982)



Summary

Model \ Criterion	EXPR	SYM	PRES	PRES ⁻¹	COMP
Linear nondeleting TOP	✗	✗	✓	✓	✓
Linear TOP	✗	✗	✓	✓	✗
Linear TOP ^R	✗	✗	✓	✓	✓
General TOP	✗	✗	✗	✓	✗
General TOP ^R	✓	✗	✗	✓	✗
Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear XTOP	✓	✗	✓	✓	✗
Linear XTOP ^R	✓	✗	✓	✓	✗
General XTOP	✓	✗	✗	✓	✗
General XTOP ^R	✓	✗	✗	✓	✗

Summary

Model \ Criterion	EXPR	SYM	PRES	PRES ⁻¹	COMP
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Linear TOP ^R	✗	✗	✓	✓	✓
General TOP	✗	✗	✗	✓	✗
General TOP ^R	✓	✗	✗	✓	✗
Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear XTOP	✓	✗	✓	✓	✗
Linear XTOP ^R	✓	✗	✓	✓	✗
General XTOP	✓	✗	✗	✓	✗
General XTOP ^R	✓	✗	✗	✓	✗
Comp. closure In-XTOP	✓	✓	✓	✓	✓
“composable” In-XTOP	?	?	✓	✓	✓

Implementation

TIBURON [MAY, KNIGHT 2006]

- Implements XTOP (and tree automata; everything also weighted)
- Framework with command-line interface
- Optimized for machine translation

Algorithms

- Application of XTOP to input tree/language
- Backward application of XTOP to output language
- Composition (for some XTOP)

Example

$qNP.NP(DT(the) N(boy)) \rightarrow NP(N(atefl))$

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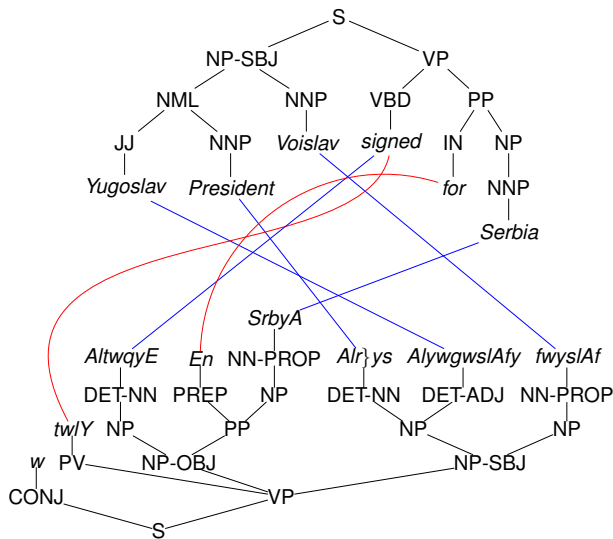
Algorithms

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Example

$qNP.NP(DT(the) N(boy)) \rightarrow NP(N(atefl))$

Multi Bottom-up Tree Transducers

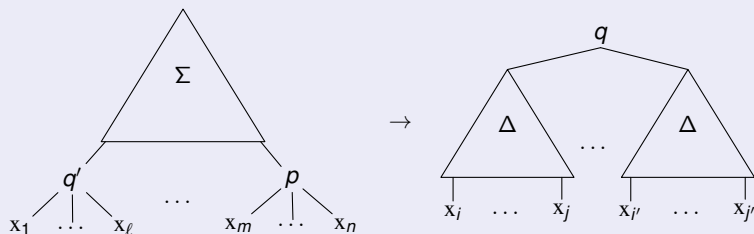


Syntax

Definition

Extended multi bottom-up tree transducer (XMBOT)

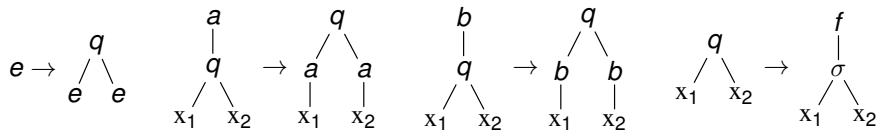
is $M = (Q, \Sigma, \Delta, F, R)$ with finitely many rules



- $q', p, q \in Q$ are now **ranked states**
- $F \subseteq Q_1$ final states

Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

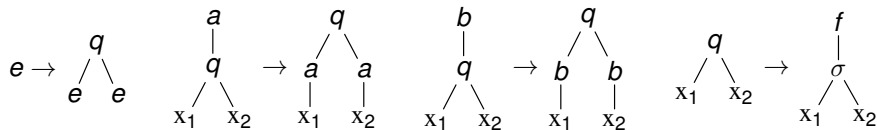


Example (Derivation)

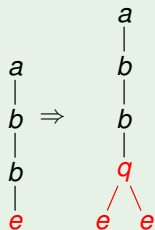
a
|
b
|
b
|
e

Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

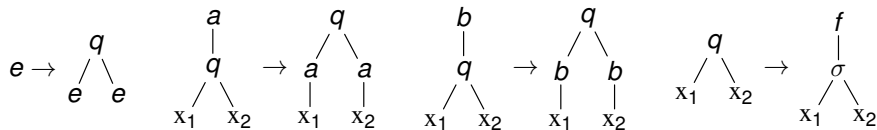


Example (Derivation)

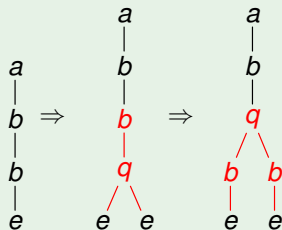


Example

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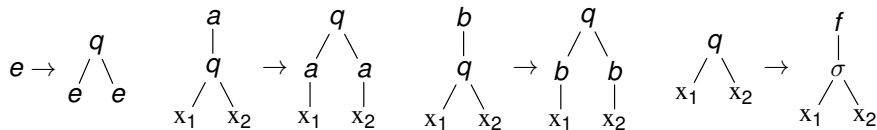


Example (Derivation)

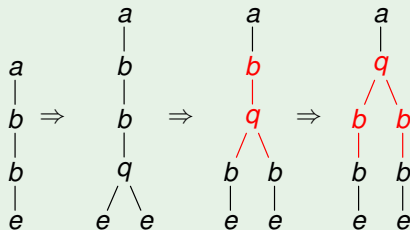


Example

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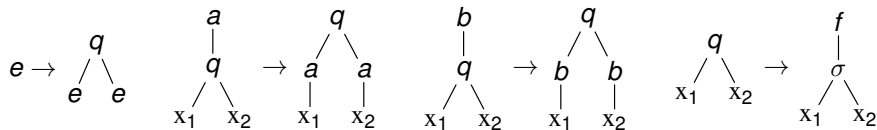


Example (Derivation)

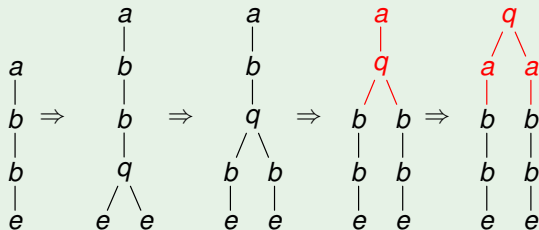


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules

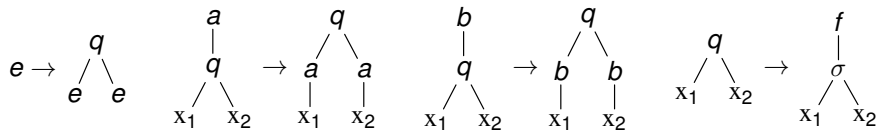


Example (Derivation)

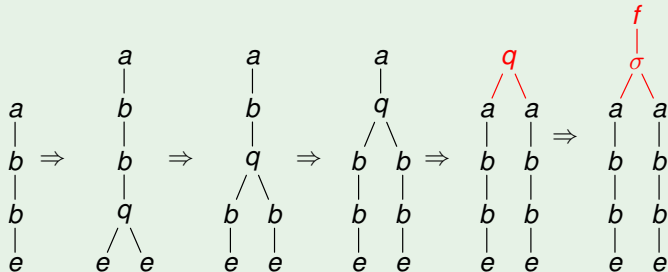


Example

States $\{f^{(1)}, q^{(2)}\}$ with final state f and rules



Example (Derivation)



Semantics

Definition

Computed transformation:

$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in F: t \Rightarrow^* q(u)\}$$

Semantics

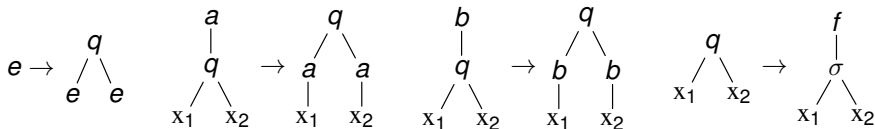
Definition

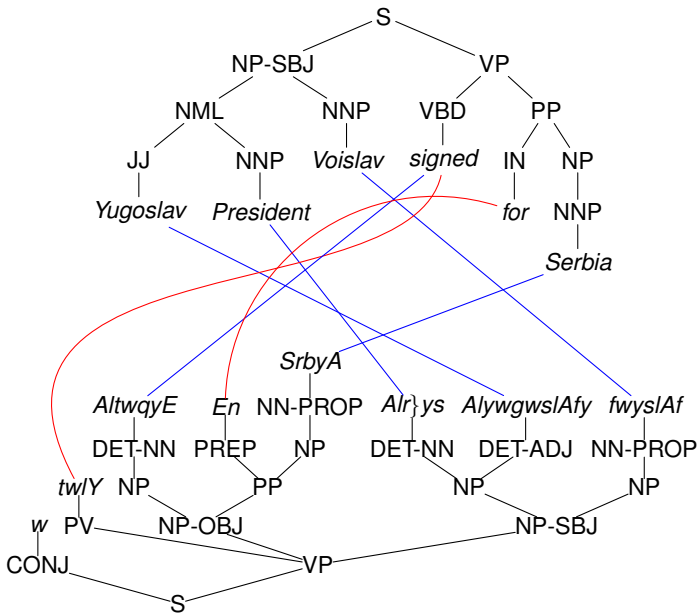
Computed transformation:

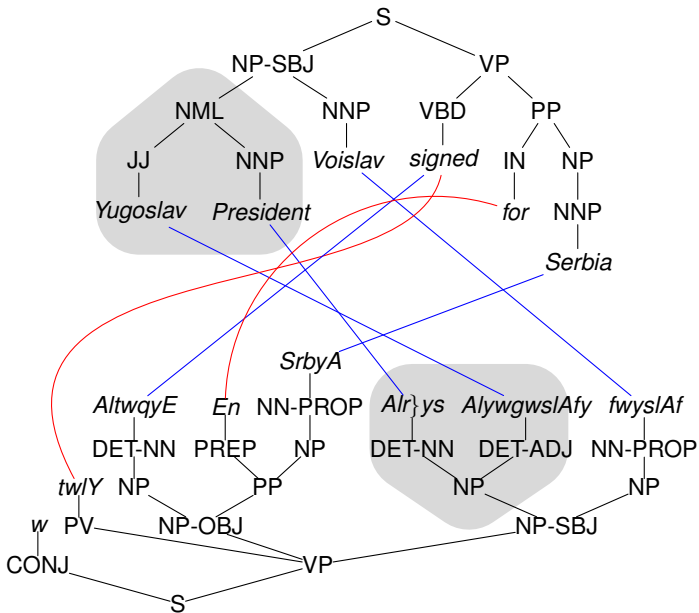
$$\tau_M = \{(t, u) \in T_\Sigma \times T_\Delta \mid \exists q \in F: t \Rightarrow^* q(u)\}$$

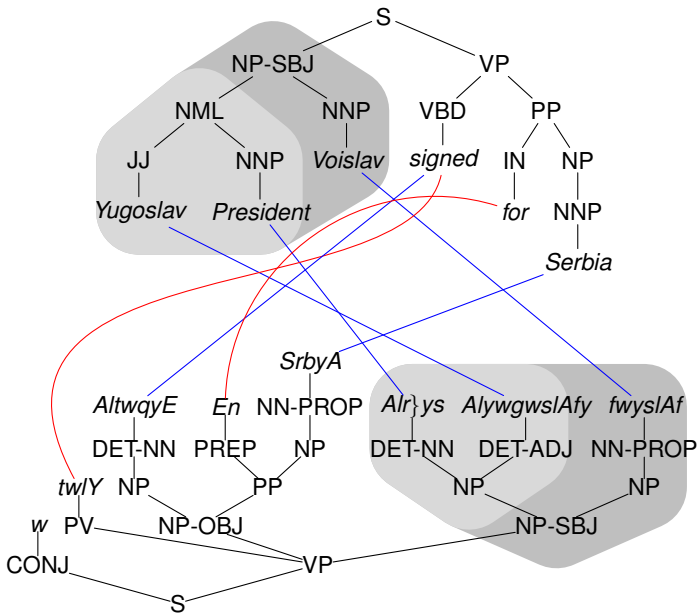
Example

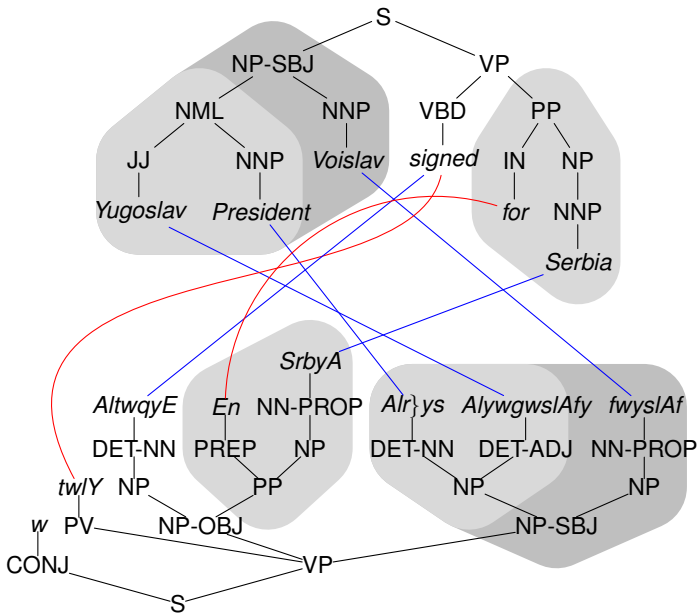
$$\tau_M = \{\langle t, \sigma(t, t) \rangle \mid t \in T_\Sigma\}$$

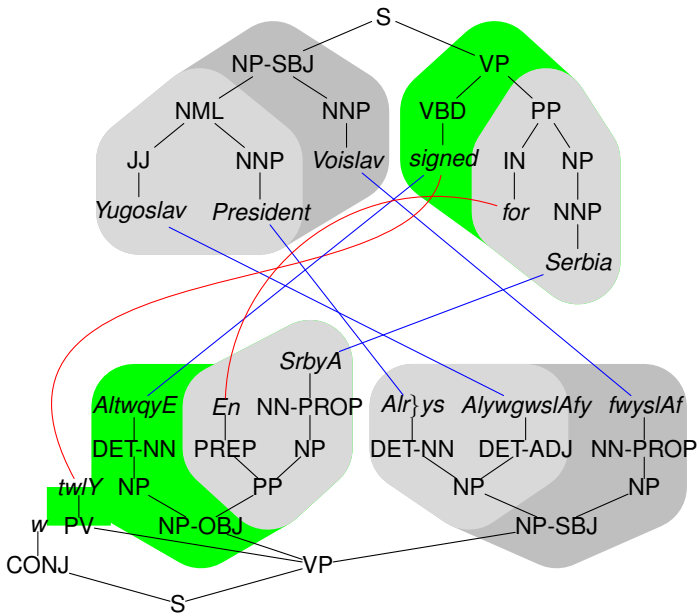




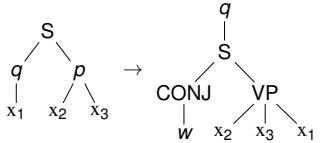
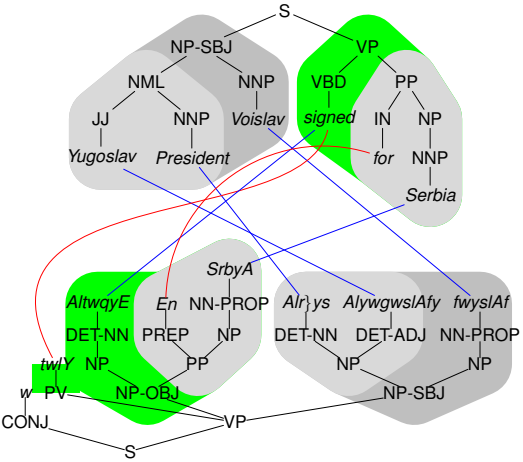




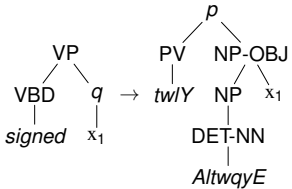
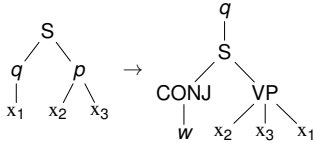
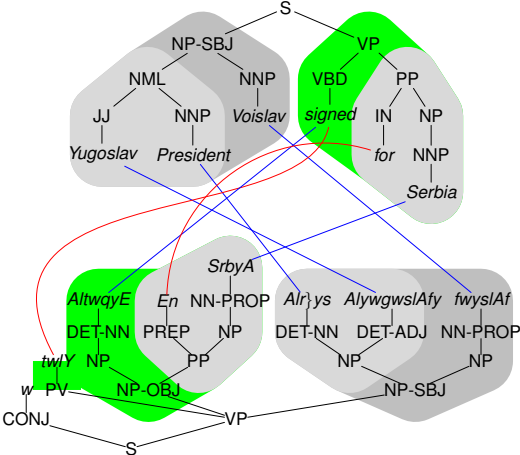




Rule extraction



Rule extraction



One-symbol normal form

Definition

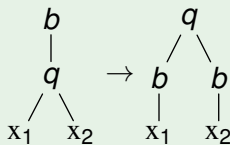
Rule in **one-symbol normal form** if it contains at most one symbol

One-symbol normal form

Definition

Rule in **one-symbol normal form** if it contains at most one symbol

Example (ENGELFRIET, LILIN, ~ 2009)

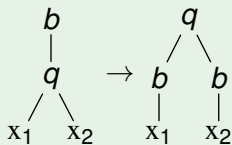


One-symbol normal form

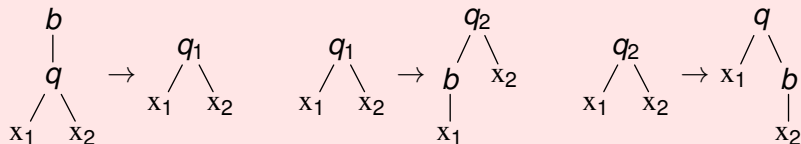
Definition

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Example (ENGELFRIET, LILIN, ~ 2009)



In one-symbol normal form



Basic properties

Example (Copying translation)

$$\tau_M = \{\langle t, \sigma(t, t) \rangle \mid t \in \mathcal{T}_\Sigma\}$$

Consequences

- XMBOT are not symmetric
- XMBOT do not preserve regularity
- but they can be composed

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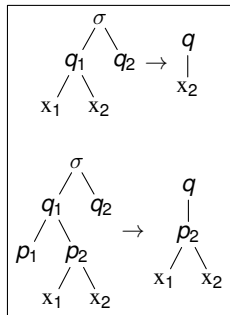
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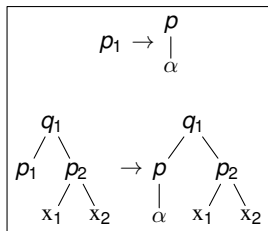
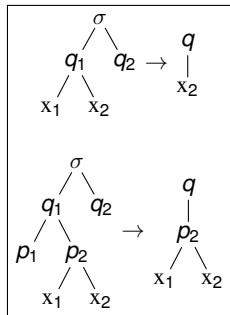
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Composition



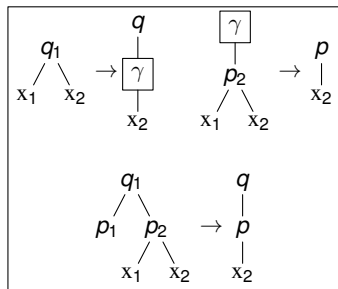
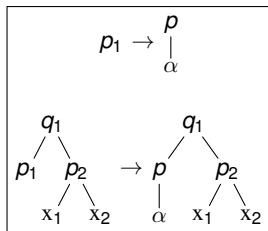
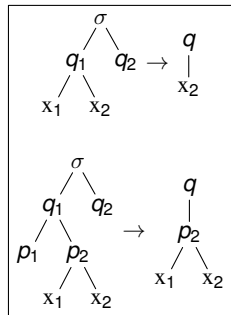
Simple composition works in the typical cases
[BAKER 1979, ENGELFRIET 1975]

Composition



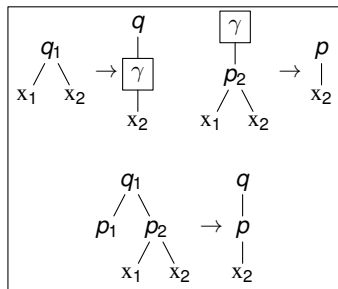
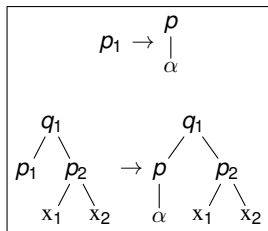
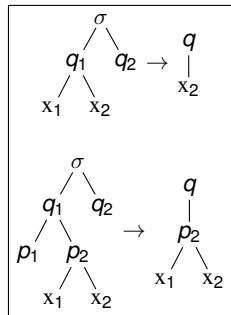
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Composition



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[BAKER 1979, ENGELFRIET 1975]

Summary

Model \ Criterion	EXPR	SYM	PRES	$PRES^{-1}$	COMP
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Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear nondeleting XMBOT	✓	✗	✗	✓	✓
Linear XMBOT	✓	✗	✗	✓	✓
General XMBOT	✓	✗	✗	✓	✗
reg.-preserving linear XMBOT	✓	✗	✓	✓	✓
invertable linear XMBOT	✓	✓	✓	✓	✓

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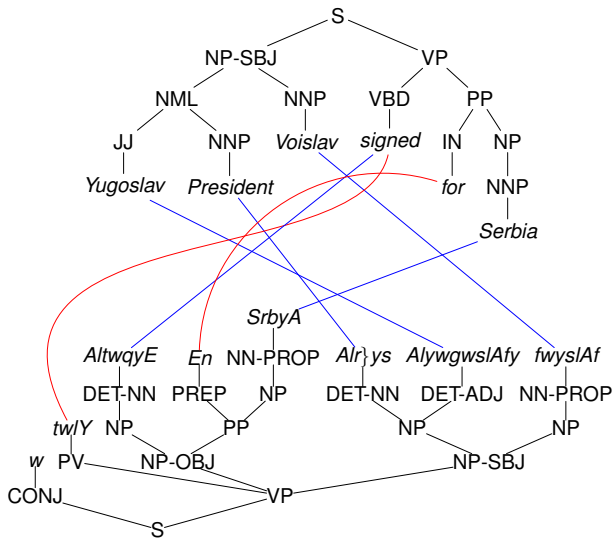
Implementation

No implementation yet,

Implementation

No implementation yet, **but stay tuned**

Synchronous Tree-Adjoining Grammars



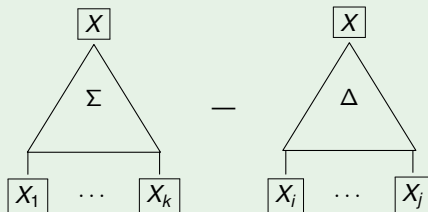
Syntax

Definition (SHIEBER, SCHABES 1990)

Synchronous tree-adjoining grammar (STAG) is $G = (N, \Sigma, \Delta, S, R)$ with a finite set R of

- substitution rules
- adjunction rules

Example (Substitution rule)



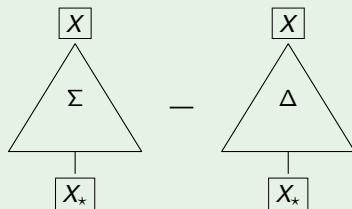
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Example (Adjunction rule)

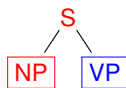
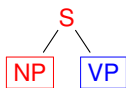


Example

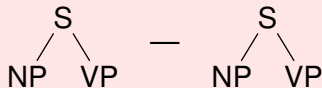
S

S

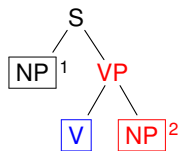
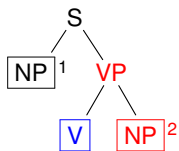
Example



Used substitution rule



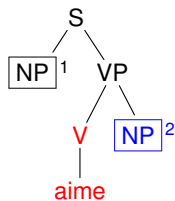
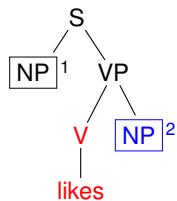
Example



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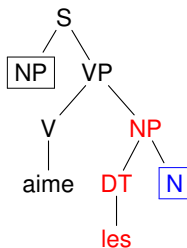
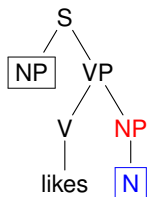
Example



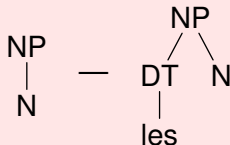
Used substitution rule

V — V
likes — aime

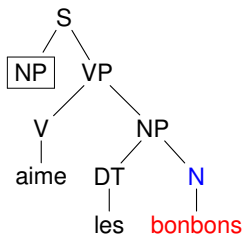
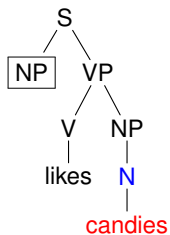
Example



Used substitution rule



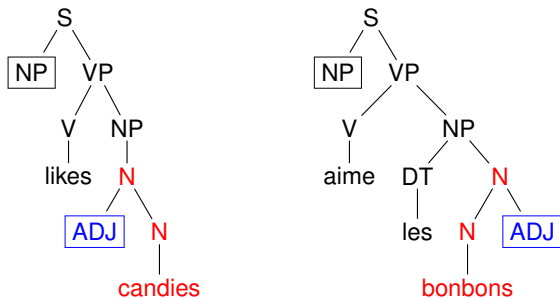
Example



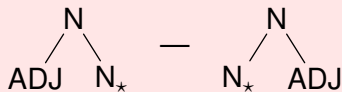
Used substitution rule

$$\begin{array}{c} \text{N} \\ | \\ \text{candies} \end{array} \quad - \quad \begin{array}{c} \text{N} \\ | \\ \text{bonbons} \end{array}$$

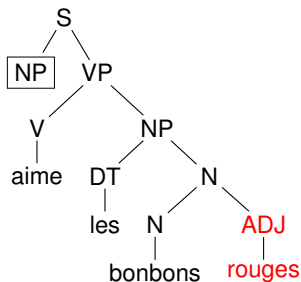
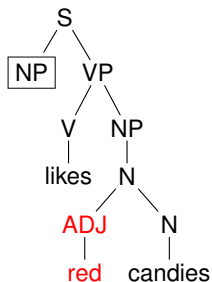
Example



Used adjunction rule



Example



Used substitution rule

ADJ — ADJ
| — |
red — rouges

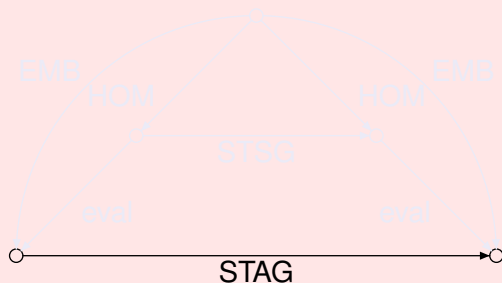
Definition

Computed transformation:

$$\tau_G = \{(t, u) \in T_\Sigma \times T_\Delta \mid (S, S) \Rightarrow^* (t, u)\}$$

Relation to tree transducers

Illustration



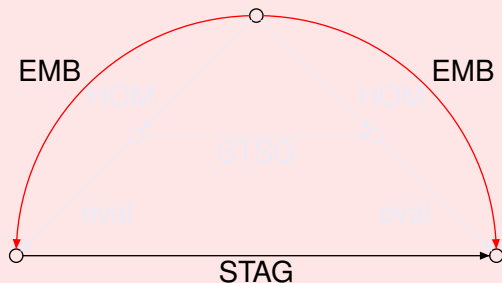
Definition (SHIEBER 2006)

embedded tree transducer is a macro tree transducer:

- linear, nondeleting, deterministic, total
- 1-parameter: linear, nondeleting

Relation to tree transducers

Illustration



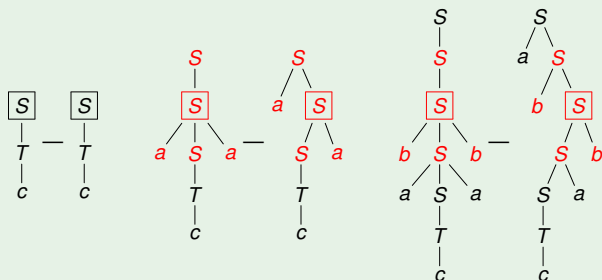
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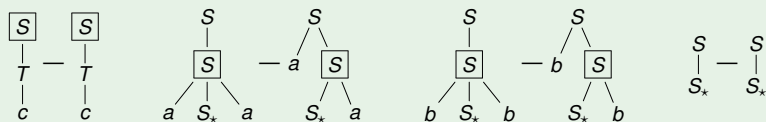
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Copying example

Example

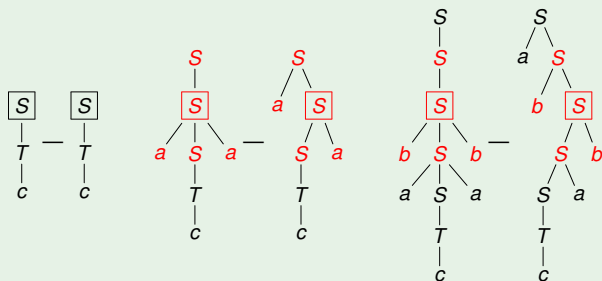


Example



Copying example

Example



String translation

$$\{(wcw^R, wcw) \mid w \in \{a, b\}^*\}$$

Basic properties

Example (Copying translation)

$$\tau_G = \{(wcw^R, wcw) \mid w \in \{a, b\}^*\}$$

Consequences

- STAG are **symmetric**
- STAG do not preserve regularity (neither direction)

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Summary

Model \ Criterion	EXPR	SYM	PRES	$PRES^{-1}$	COMP
Linear nondeleting TOP	✗	✗	✓	✓	✓
Linear nondeleting XTOP	✓	✓	✓	✓	✗
Linear nondeleting XMBOT	✓	✗	✗	✓	✓
Linear XMBOT	✓	✗	✗	✓	✓
General XMBOT	✓	✗	✗	✓	✗
reg.-preserving linear XMBOT	✓	✗	✓	✓	✓
invertable linear XMBOT	✓	✓	✓	✓	✓
STAG	✓	✓	✗	✗	✗

Implementation

XTAG [THE XTAG PROJECT 2008]

- Implements TAG, STAG
- Optimized for natural language applications
- Application of STAG

<http://www.cis.upenn.edu/~xtag/>

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References

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